

```
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 1.0f - 0.5f * nnt)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn > 0.5f ? 1 : -1));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, R, Align;
    e.x + radiance.y + radiance.z );
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}
```

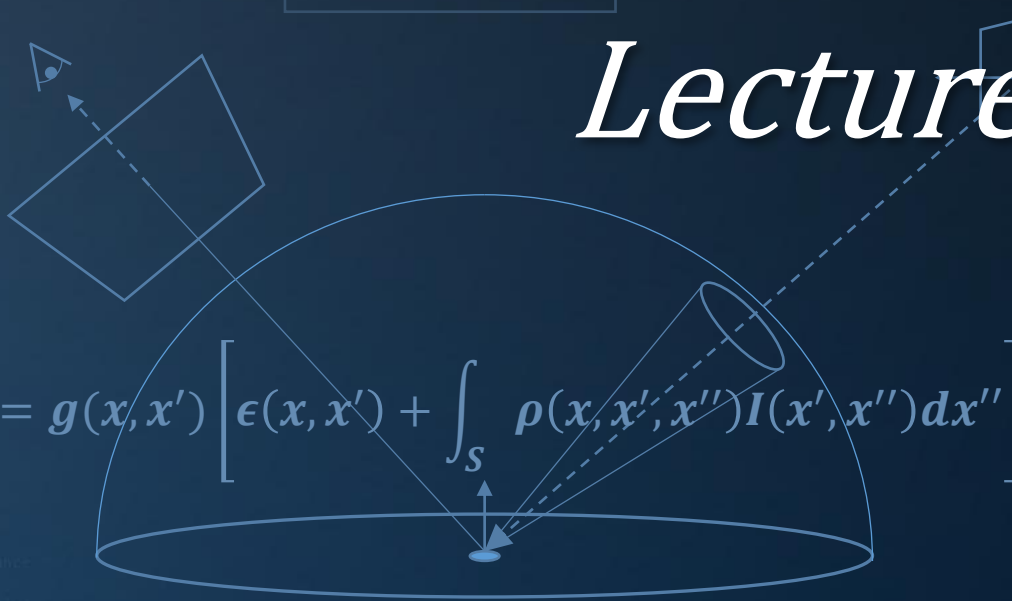


INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 - February 2023

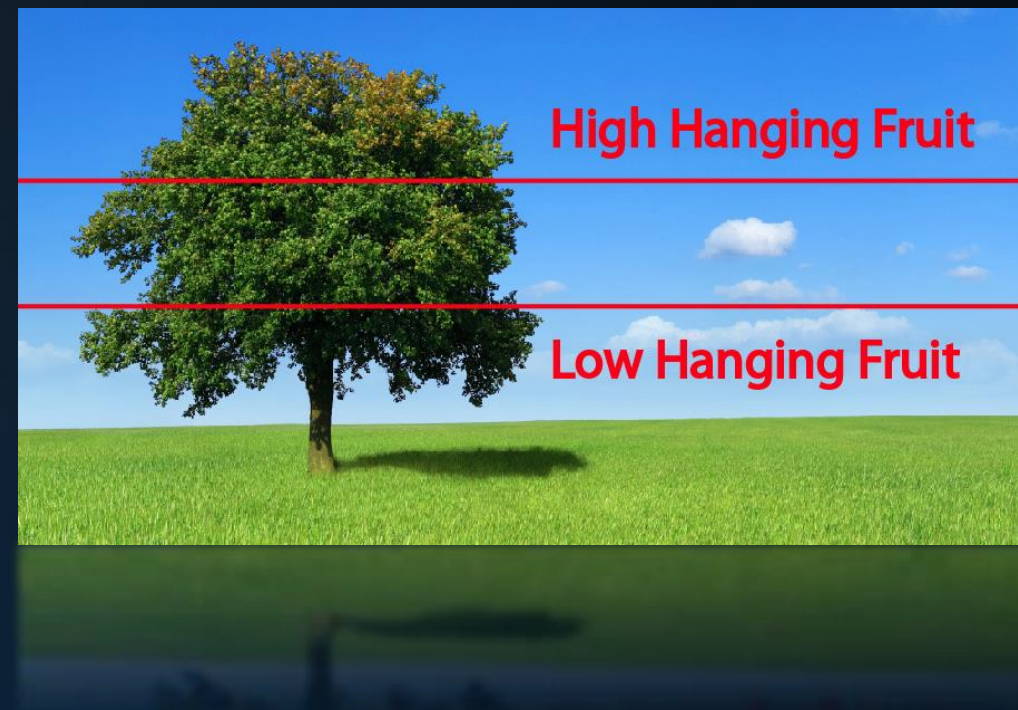
Lecture 11 - “Various”

Welcome!



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox & IS
- Normal Maps
- Microfacets



Gamma Correction

Human Eye

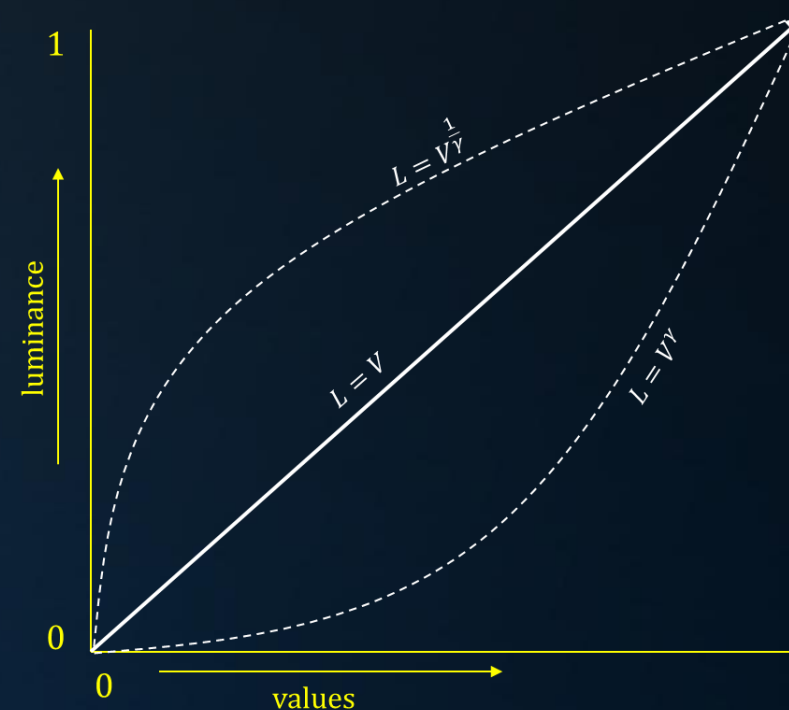
Digital representation of intensities is discrete: for ARGB32, we have 256 levels for red, green and blue.

The human eye is more sensitive to differences in luminance for dark shades. When encoding luminance, it is advantageous to have more detail in the lower regions, e.g.:

$$L = rgb^\gamma \Rightarrow rgb = L^{\frac{1}{\gamma}}$$

For the human eye, $\gamma = 2.33$ is optimal*.

*: Ebner & Fairchild, Development and testing of a color space (IPT) with improved hue uniformity, 1998.



Gamma Correction

CRT Power Response

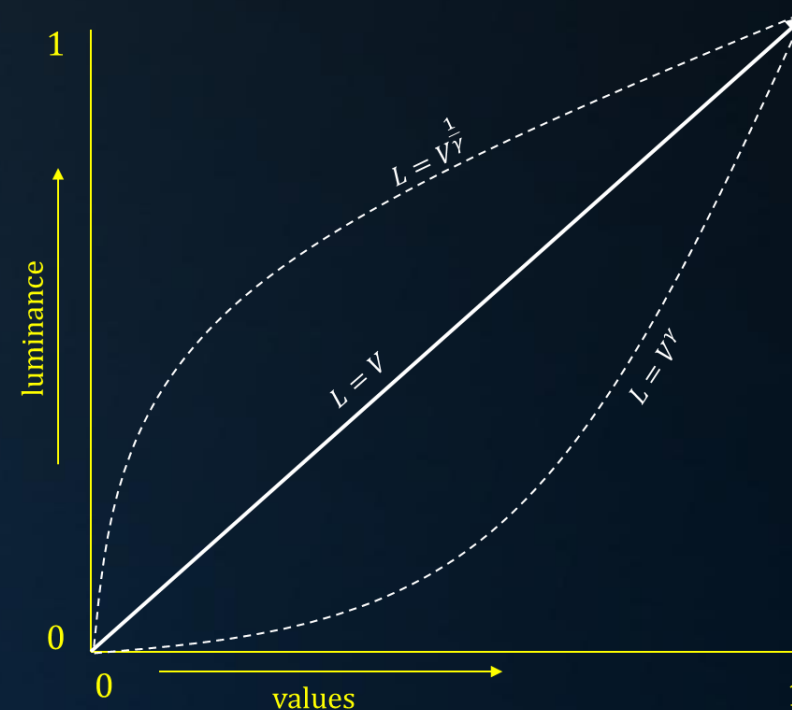
A classic CRT display converts incoming data to luminance in a non-linear way.

$$L = rgb^\gamma \Rightarrow rgb = L^{\frac{1}{\gamma}}$$

For a typical monitor, $\gamma = 2.2$.

In other words:

- If we encode our luminance using $rgb = L^{\frac{1}{\gamma}}$, it will appear linear on the monitor.
- At the same time, this yields a distribution that has more detail for darker shades, which suits the human eye.



Gamma Correction

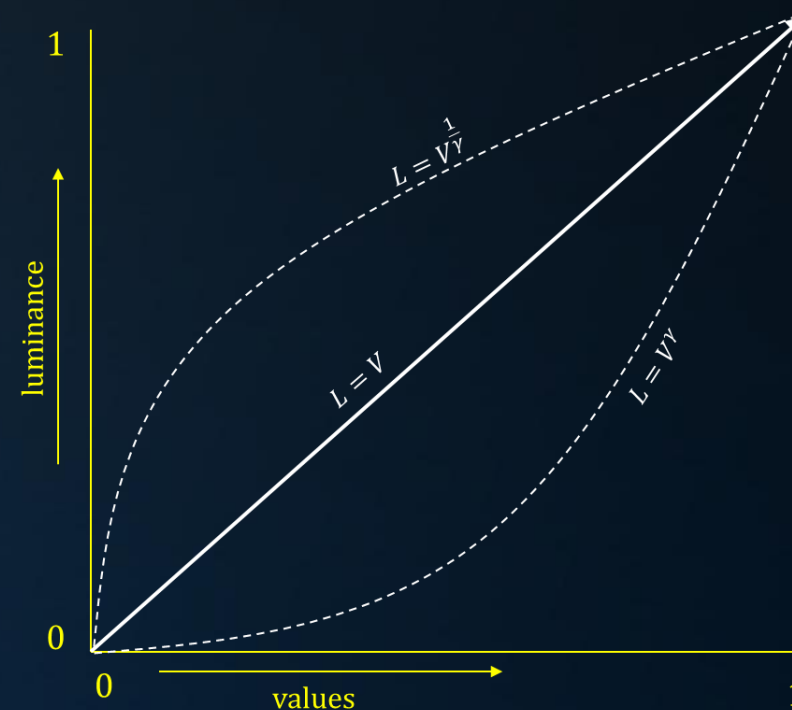
Practical Gamma Correction

To ensure linear response of the monitor to our synthesized images, we feed the monitor adjusted data:

$$rgb = L^{1/2.2} \approx \sqrt{L}$$

What happens if we don't do this?

1. L will be $rgb^{2.2}$; the image will be too dark.
2. A linear gradient will become a quadratic gradient; a quadratic gradient will become a cubic gradient
 → your lights will appear to have a very small area of influence.

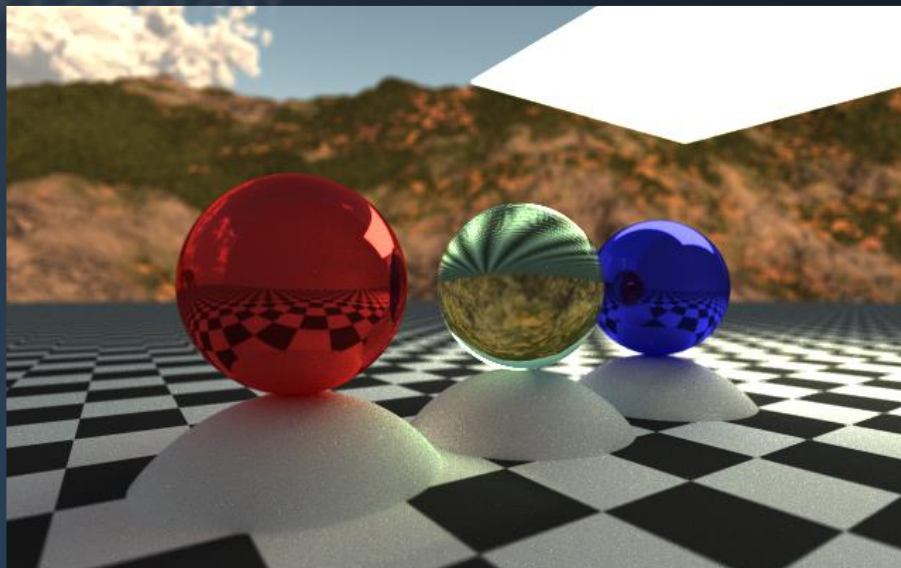


Gamma Correction

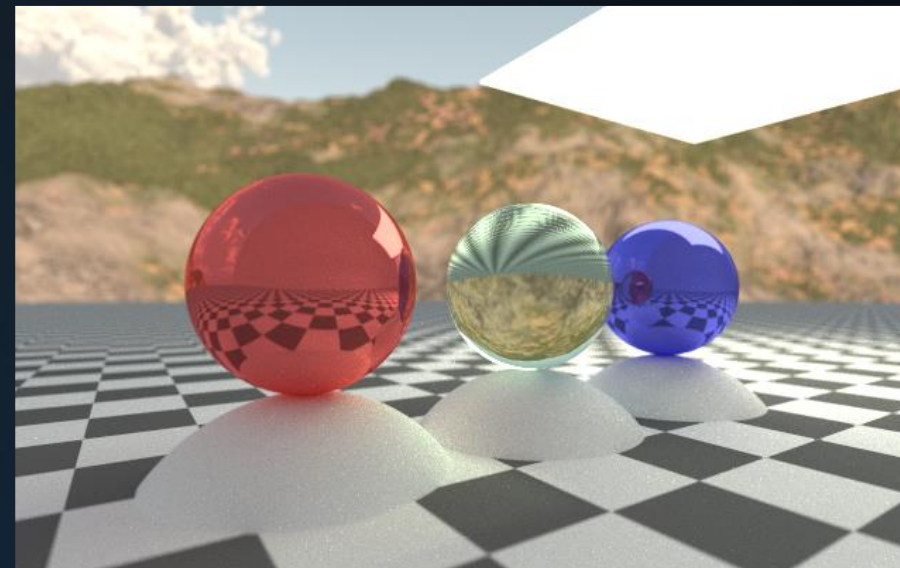
```

ics
& (depth < MAXDEPTH)
{
    nt = inside ? 1.0 : 0.0;
    nt = nt / nc; ddn = dot(N, L);
    cos2t = 1.0f - nnt * nnt;
    D, N );
    0);
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) *
    Tr) R = (D * nnt - N * (ddn
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &light
    e.x + radiance.y + radiance.z ) > 0) && (depth
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (r
    random walk - done properly, closely following
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2,
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

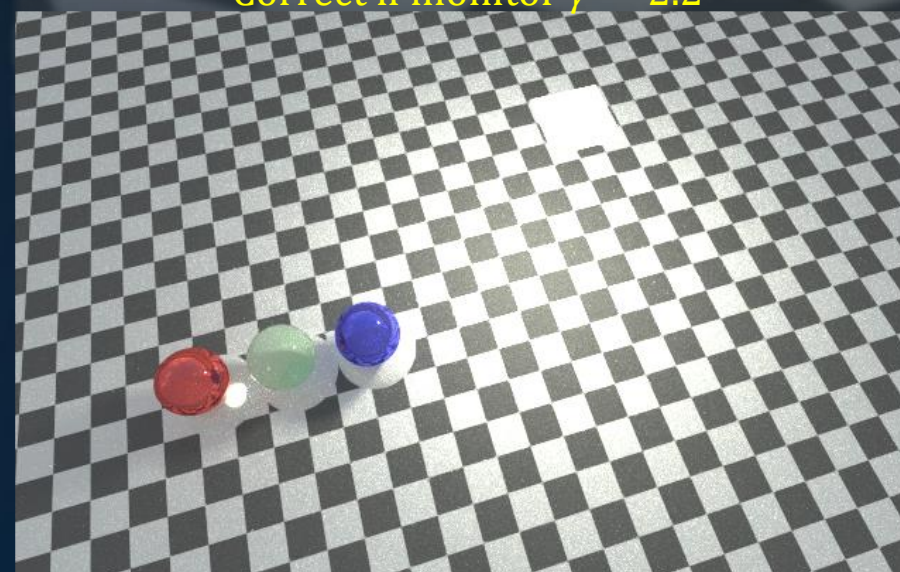
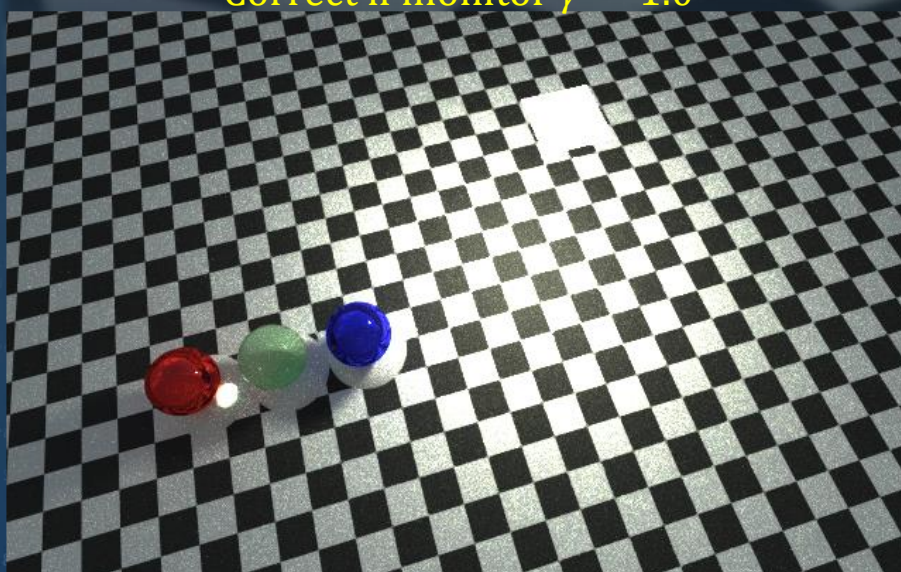
```



Correct if monitor $\gamma = 1.0$



Correct if monitor $\gamma = 2.2$



Gamma Correction

Legacy

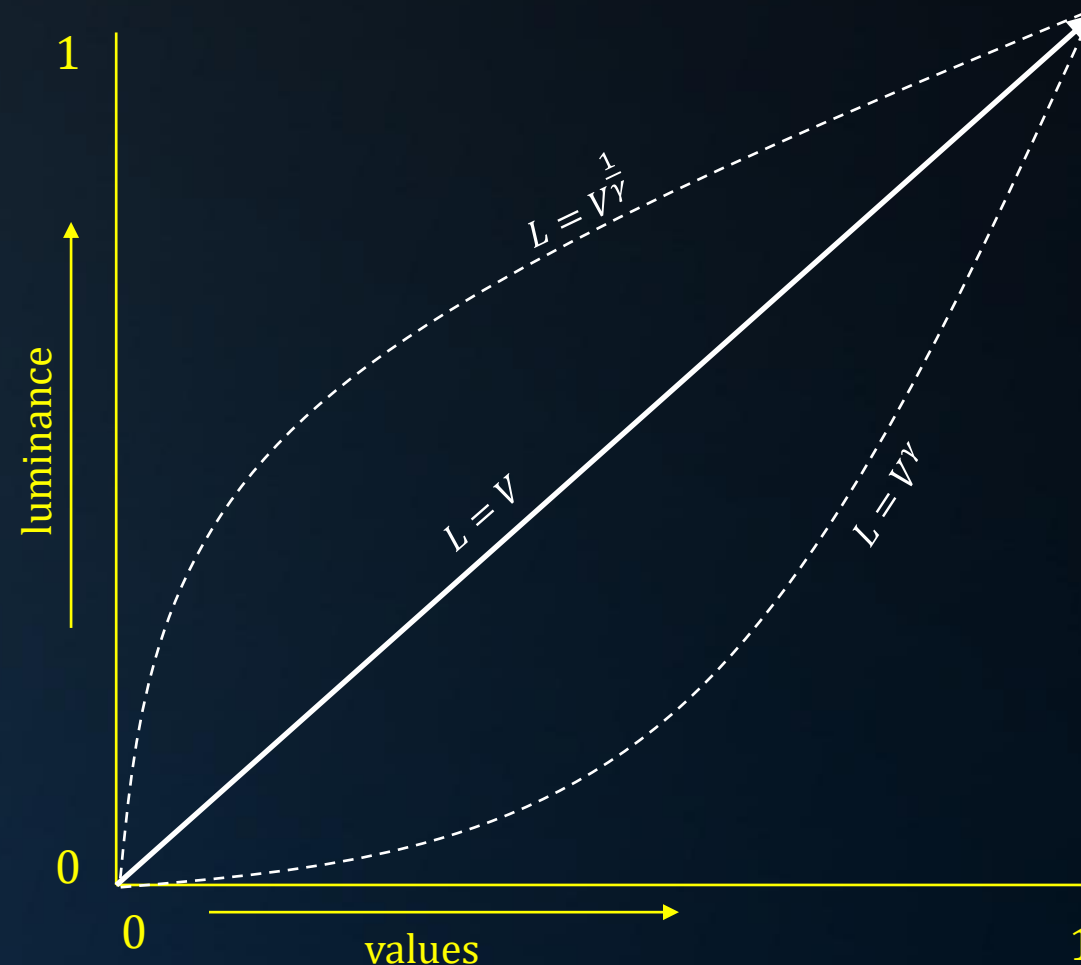
The response of a CRT is $L = V^{2.2}$; what about modern screens?

Typical laptop / desktop screens have a linear response, but expect applications to provide $\sqrt{L}$ data... So V is modified (in hardware, or by the driver): $V = V^2$.

$$L \Rightarrow \sqrt{L} \Rightarrow L^2$$

Not all screens take this legacy into account; especially beamers will often use $\gamma = 1$.

Gamma correct only if the hardware or video driver expects it!

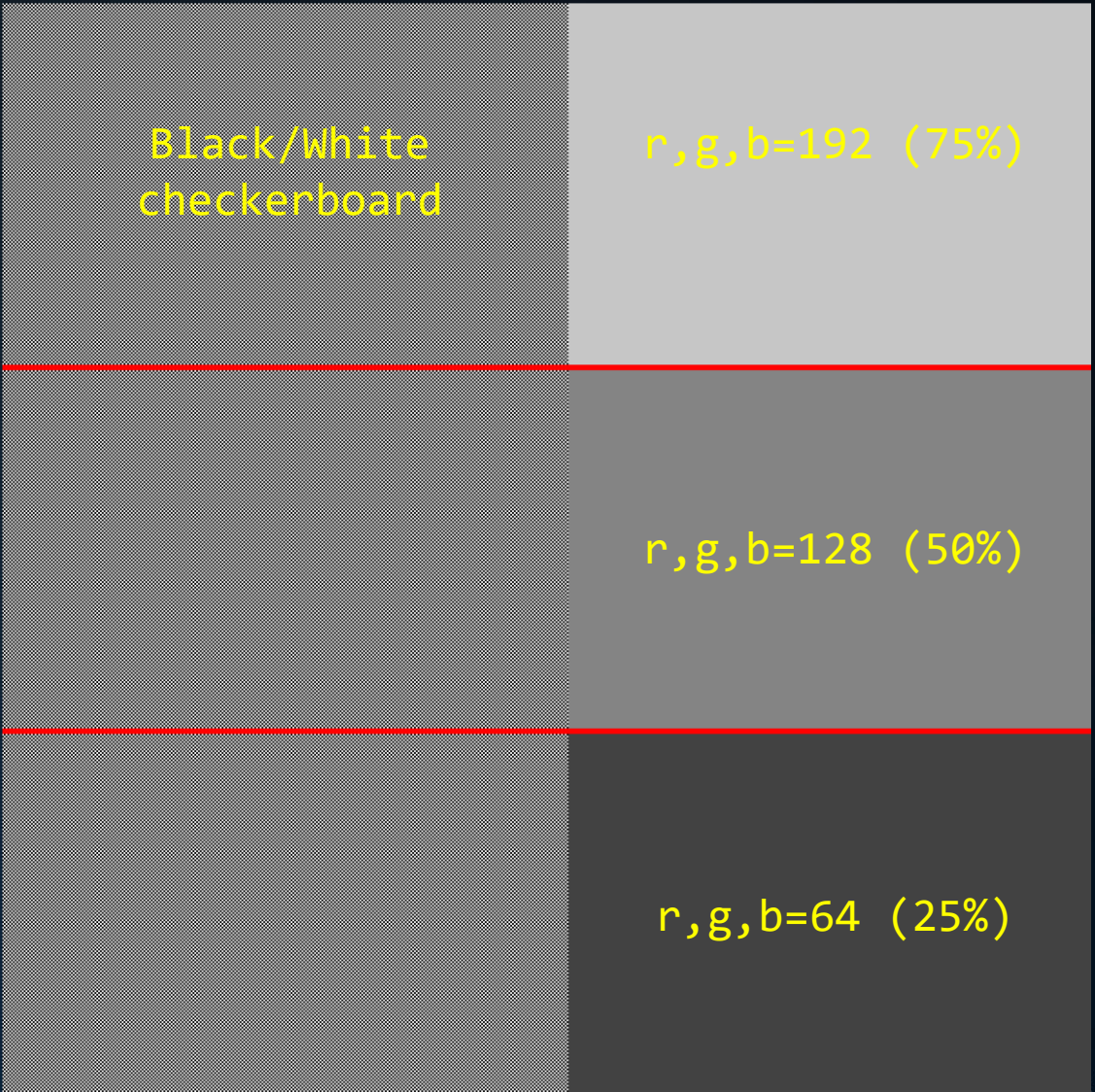


Gamma Correction

Gamma Corrected Or Not?

Open gamma.gif using the windows image previewer and zoom to the smallest level (1:1). Which bar in the right column is most similar in brightness to the right column?

	$\gamma=1$	$\gamma=2$
75%	0.75	0.56
50%	0.50	0.25
25%	0.25	0.06



Gamma Correction

Consequences

How are your digital photos / DVD movies stored?

1. With gamma correction, ready to be sent to a display device that expects $\sqrt{L}$
2. Without gamma correction, expecting the image viewer to apply $\sqrt{L}$

For jpegs and mpeg video, the answer is 1: these images are already gamma corrected.

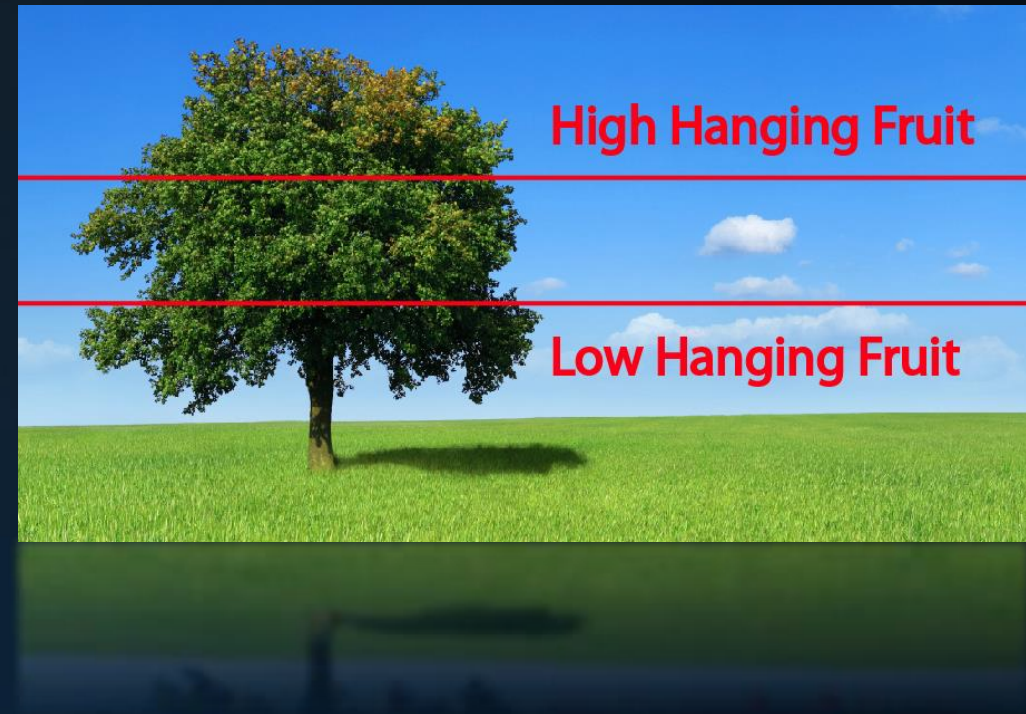
➔ Your textures may require conversion to linear space:

$$L = rgb^2$$



Today's Agenda:

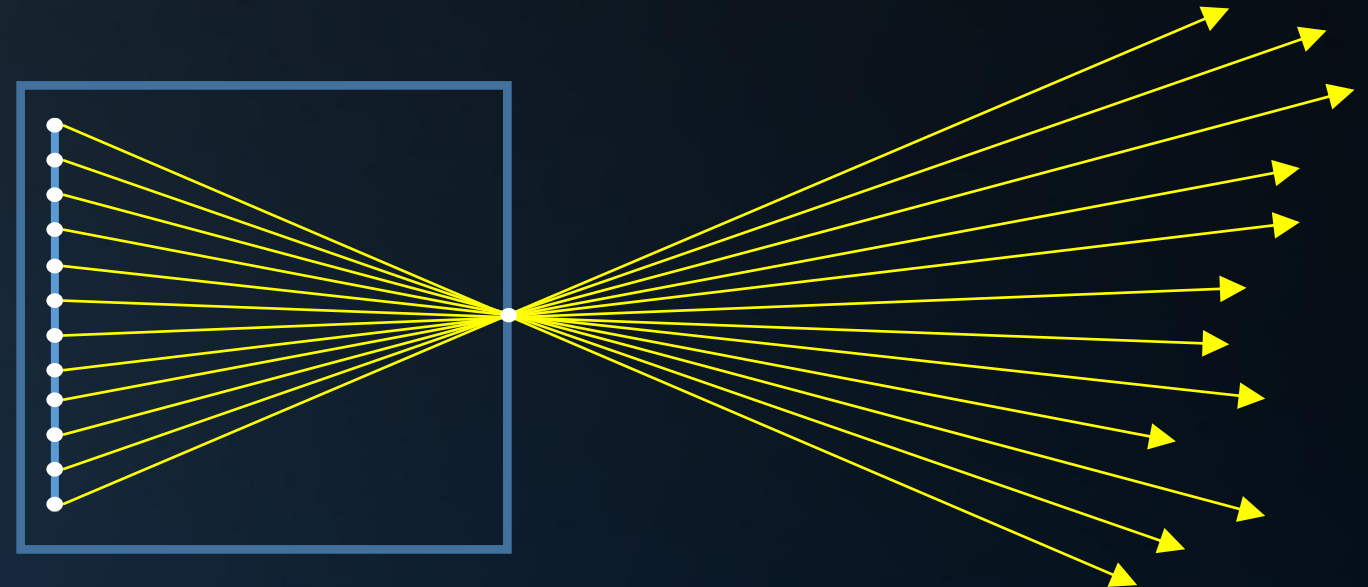
- Gamma Correction
- Depth of Field
- Skybox & IS
- Normal Maps
- Microfacets



Depth of Field

Focus

A pinhole camera ensures that each pixel receives light from a single direction.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, N);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * cos2t);
        Tr) R = (D * nnt - N * (ddn * cos2t));
    }
    E * diffuse;
    = true;
}

efl + refr) && (depth < MAXDEPTH)
{
    D, N );
    refl * E * diffuse;
    = true;
}

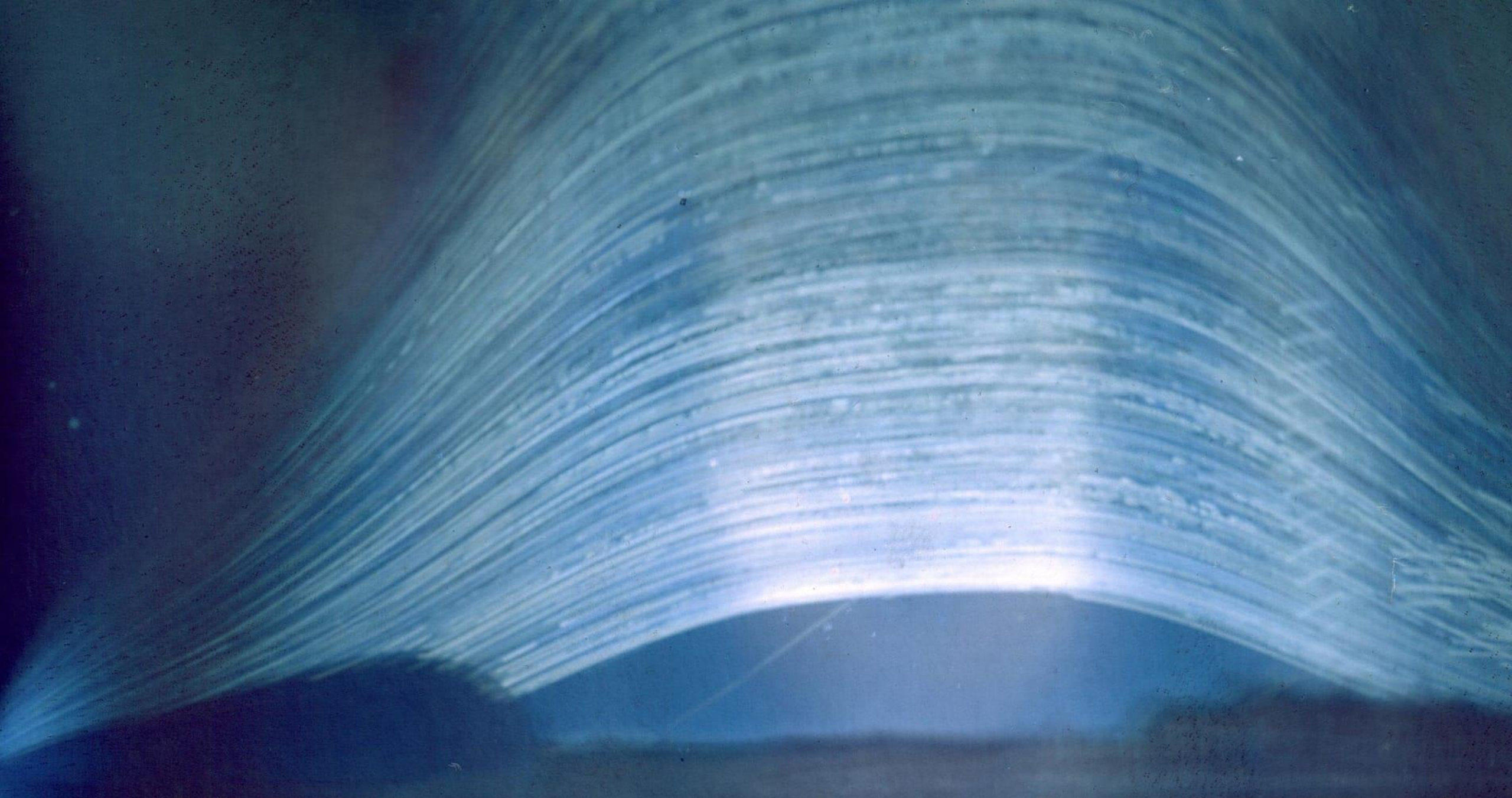
MAXDEPTH)

survive = SurvivalProbability( diffuse );
estimation - doing it properly, closely following Small's
if;
radiance = SampleLight( &rand, I, &L, &light );
e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
{
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
}

random walk - done properly, closely following Small's
ive)
;
at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
survive;
pdf;
n = E * brdf * (dot( N, R ) / pdf);
sion = true;

```







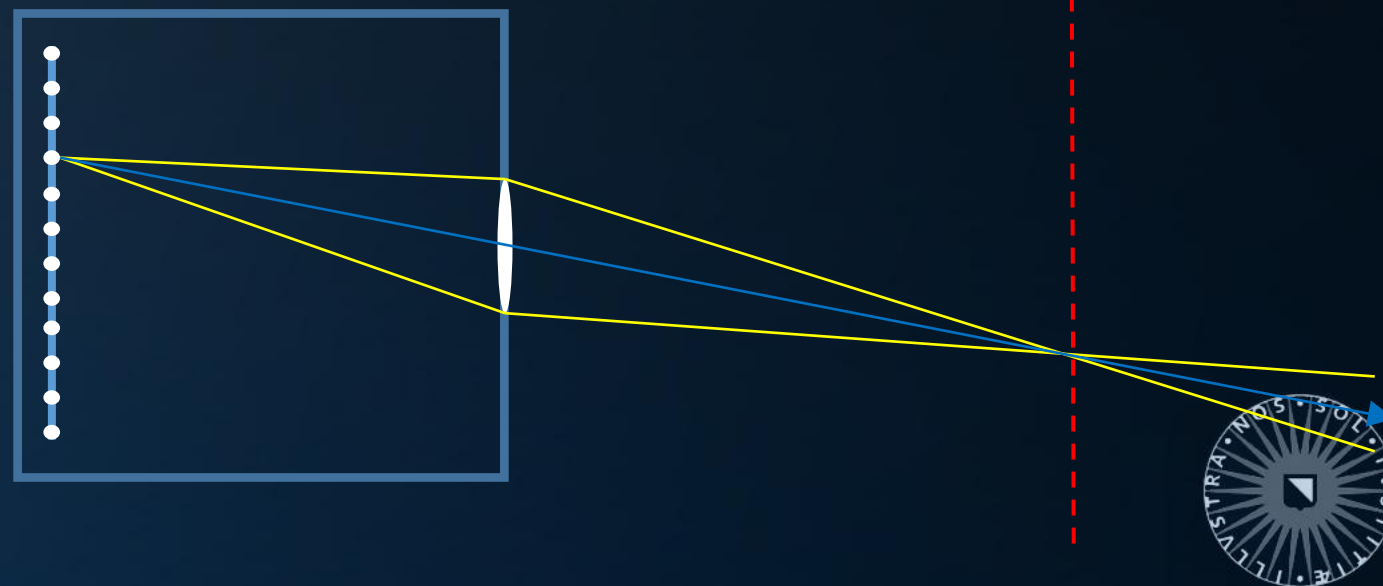
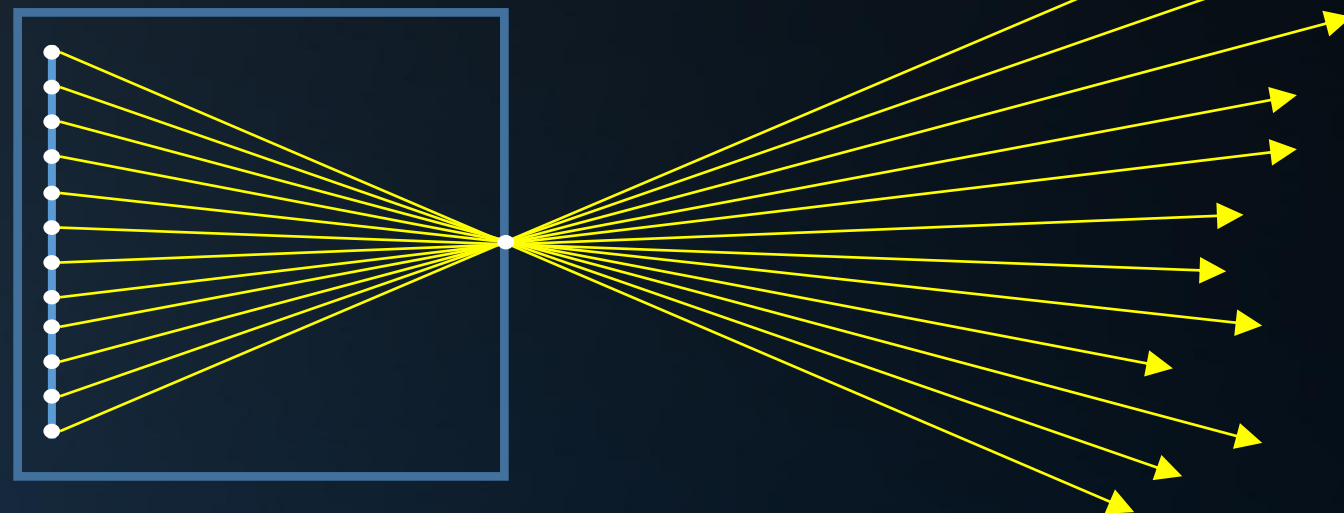
Depth of Field

Focus

A pinhole camera ensures that each pixel receives light from a single direction.

For a true pinhole, the amount of light is zero – obviously.

Actual cameras use a lens system to direct a limited set of directions to each pixel.



Depth of Field

Focus

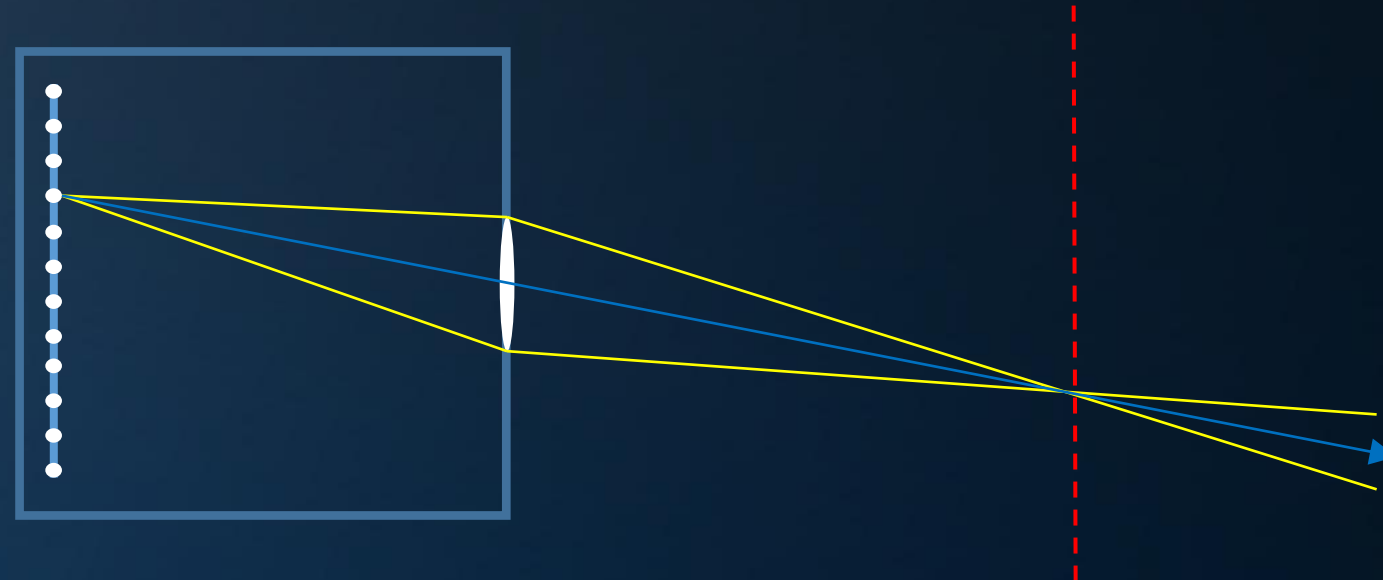
Objects on the focal plane appear in focus:

Light reflected from these objects to the lens end up on a single pixel on the film.

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    E * diffuse;
    = true;
    refl + refr) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    if;
    radiance = SampleLight( &rand, I, &L, &light, &N, &N );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    (survive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



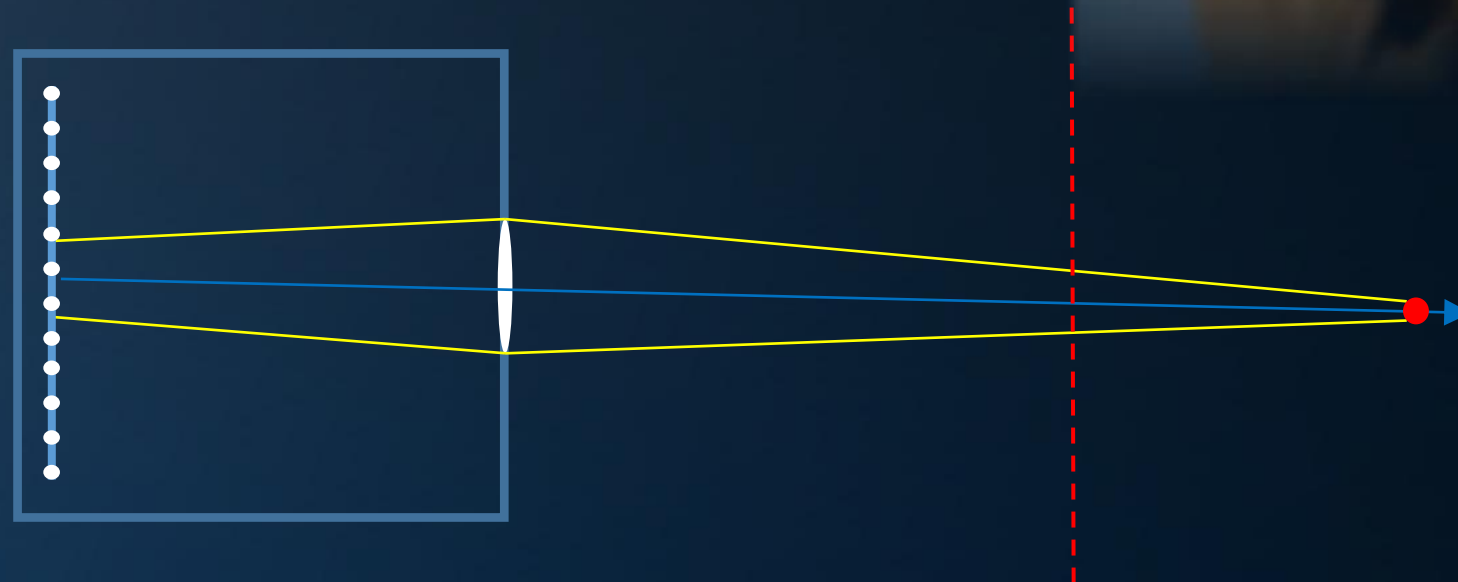
Depth of Field

Focus

Objects beyond the focal plane appear out of focus:

Light reflected from these objects is spread out over several pixels on the film: the *Circle of Confusion (CoC)*.

Something similar happens for objects before the focal plane.



Depth of Field

Circle of Confusion

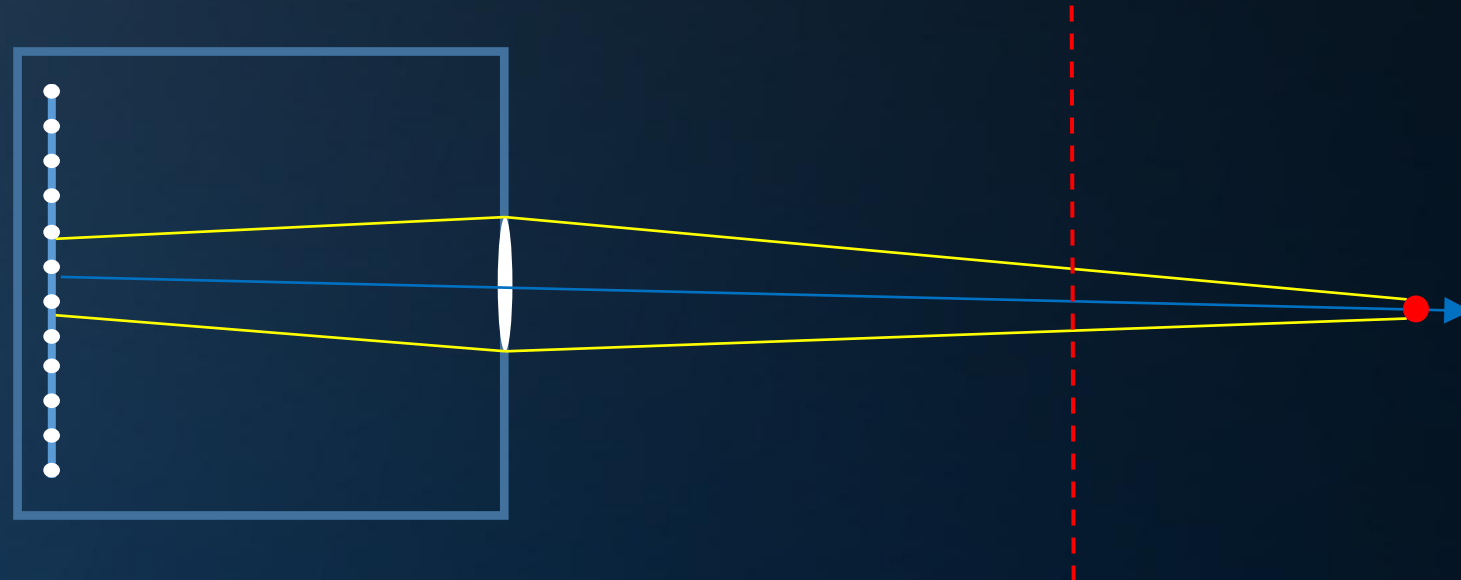
Ray tracing depth of field:

Calculate the diameter of the CoC for a distance along the primary ray, then spread out the energy over multiple pixels within a circle.

```

ics
& (depth < MAXDEPTH)
{
    if ( ! inside ) return 0;
    nt = nt / nc; ddn = ddn * ddn;
    cos2t = 1.0f - nnt * ddn;
    D, N );
    )
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * cos2t);
        Tr) R = (D * nnt - N * (ddn * cos2t));
    }
    E * diffuse;
    = true;
    -
    refl + refr) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following Small's
    if;
    radiance = SampleLight( &rand, I, &L, &light, &N, &N );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
}

```



Depth of Field

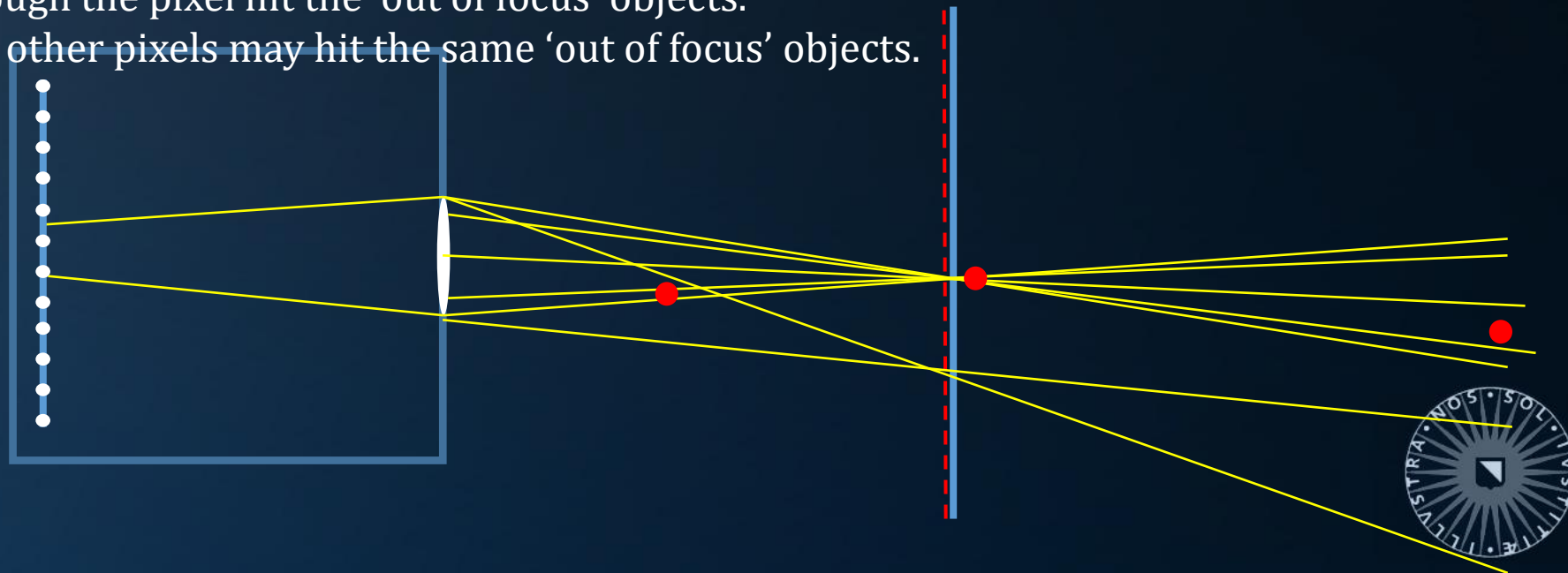
Circle of Confusion

Efficient depth of field:

We place the virtual screen plane at the focal distance (from the lens).

Rays are generated on the lens, through each pixel.

- All rays through the pixel will hit the object near the focal plane;
- Few rays through the pixel hit the 'out of focus' objects.
- Rays through other pixels may hit the same 'out of focus' objects.



Depth of Field

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * f);
        Tr) R = (D * nnt - N * (ddn * cos2t));
    }
    E * diffuse;
    = true;
    -
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, 1 -
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &light,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psum;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Smith's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```

Generating Primary Rays

Placing the virtual screen plane at the focal distance:

Recall that a 2×2 square at distance d yielded a FOV that could be adjusted by changing d .

We can adjust d without changing FOV by scaling the square and d by the same factor.

Random point on the lens: generate an (ideally uniform) random point on a disc. This is non-trivial; see Global Illumination Compendium, 19a or b. Alternatively, you can use rejection sampling.

Also nice: replace the disc with a regular n-gon.

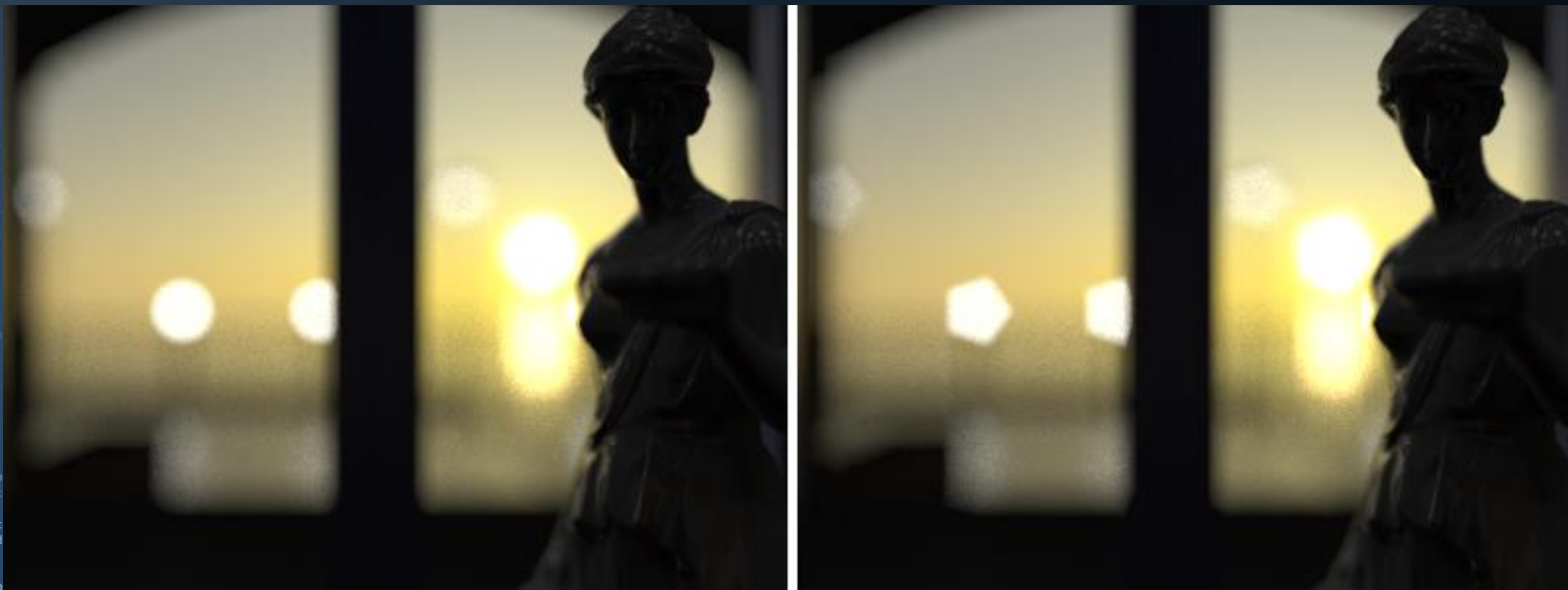


Depth of Field

```

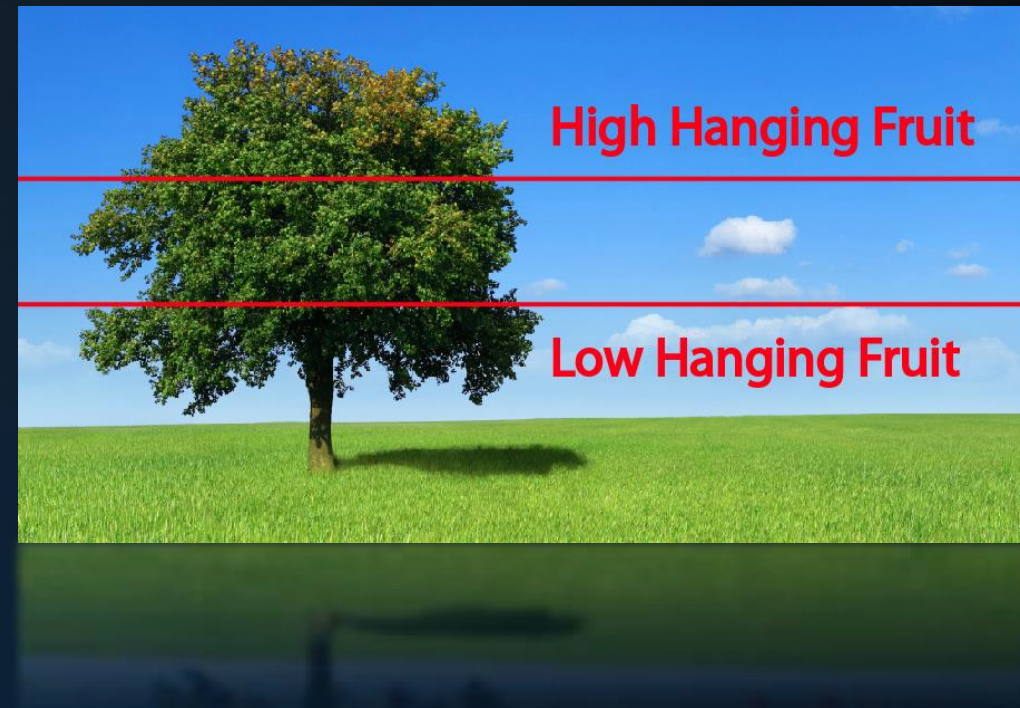
ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt;
        at Tr = 1 - (R0 + (1 - R0) * f);
        R = (D * nnt - N * a);
        E * diffuse;
        = true;
    }
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability - doing it
    if;
    radiance = SampleLight(x, y, z, radiance.x + radiance.y + radiance.z);
    w = true;
    at brdfPdf = EvaluateDf;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance.x + radiance.y + radiance.z);
    random walk - done properly, closely following the path of the photon
    (live)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox
- Spots, IES Profiles
- Microfacets



Skybox

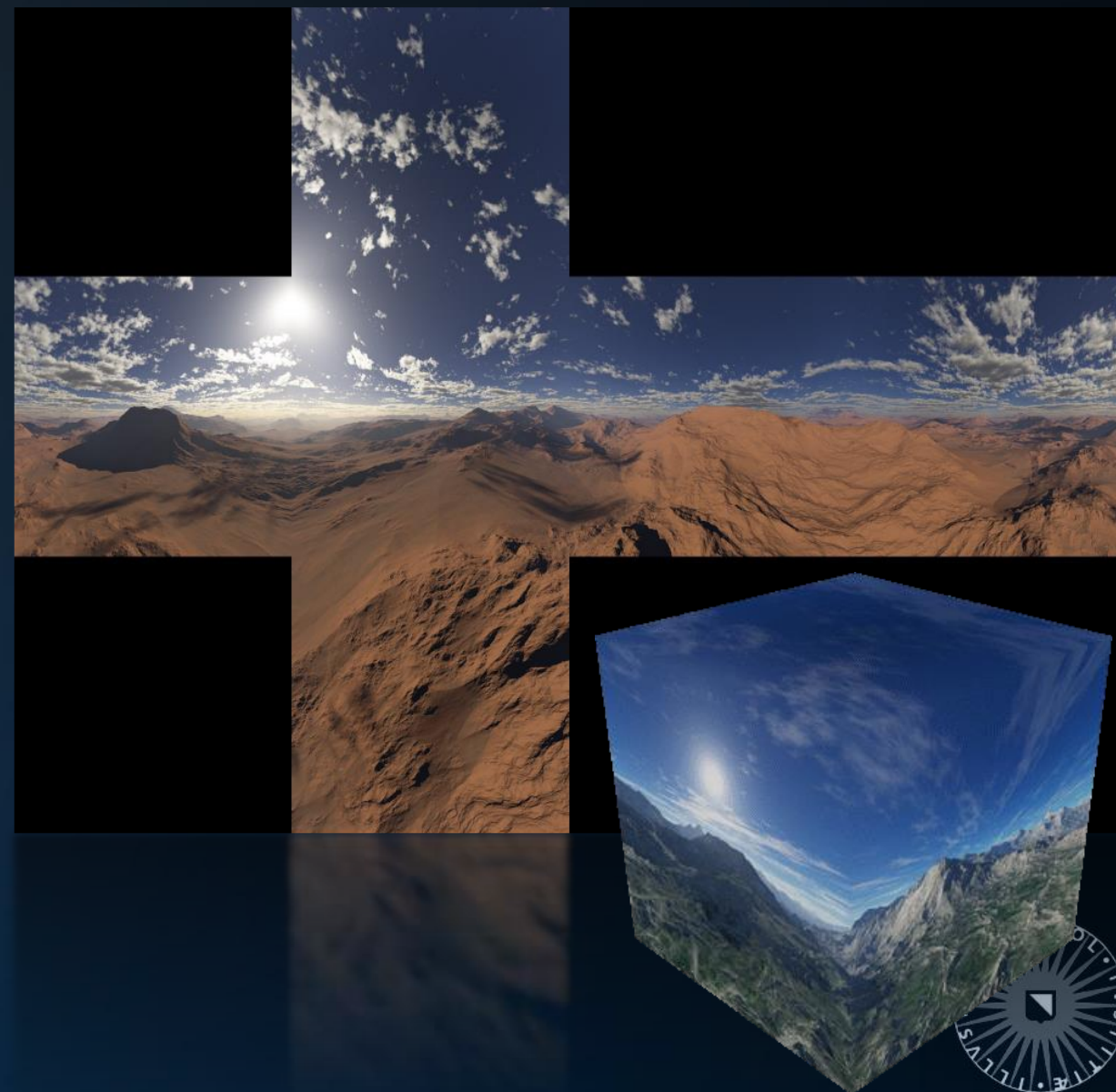
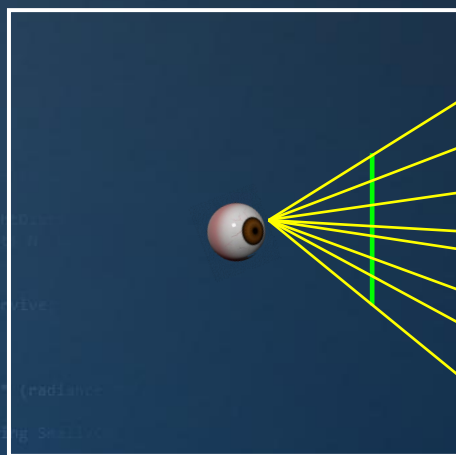
Environment Imposter

Many games use a skybox to simulate distant geometry without actually storing this geometry.

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * ddn;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    Tr) R = (D * nnt - N * (ddn * cos2t));
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, 1);
    estimation - doing it properly, closely following
    f;
    radiance = SampleLight( &rand, I, &L, &align, &pdf, &pdf);
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Pdf;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf);
        random walk - done properly, closely following
        (survive)
    }
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf);
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;
}

```



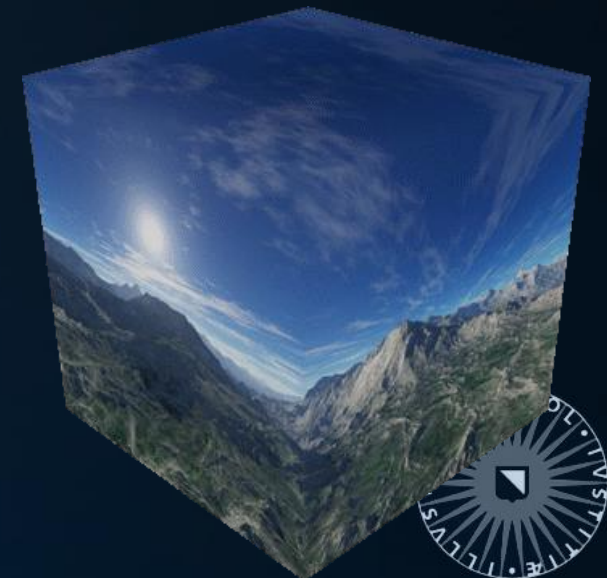
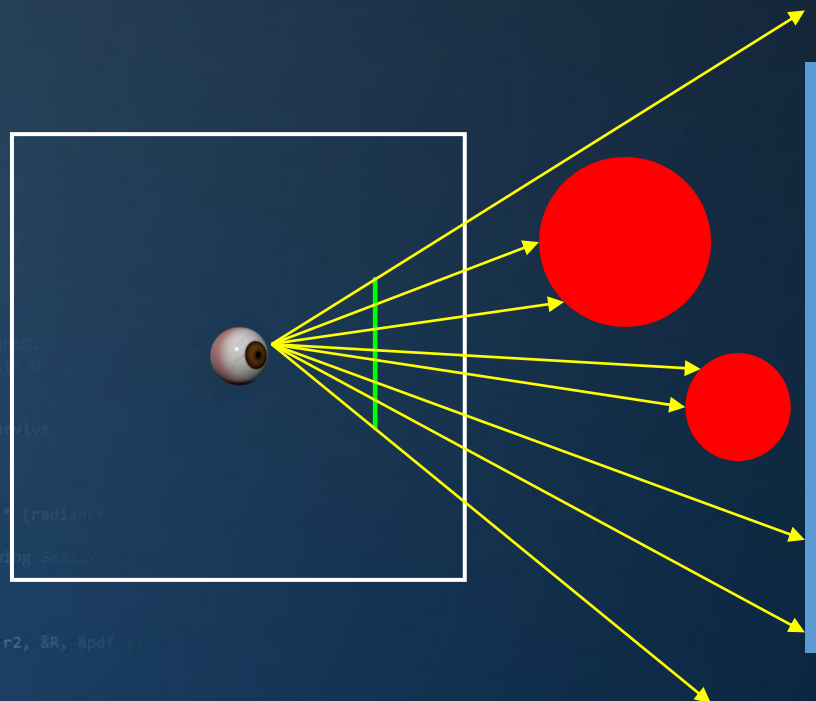
Skybox

Environment Imposter

Many games use a skybox to simulate distant geometry without actually storing this geometry.

The skybox is a $1 \times 1 \times 1$ box centered around the camera: assuming the sky is at an ‘infinite’ distance, the location of the camera inside this box is irrelevant.

Which face of the cubemap we need to use, and where it is hit by a ray is determined on ray direction alone.



Skybox

High Dynamic Range

Instead of using a skybox, we can also use an equirectangular mapping, which maps azimuth to u and elevation to v :

$$\theta = \pi(u - 1), \varphi = \pi v; \quad u = [0,2], \quad v = [0,1].$$

Converting polar coordinates to a unit vector:

$$\vec{D} = \begin{pmatrix} \sin(\varphi)\sin(\theta) \\ \cos(\varphi) \\ -\sin(\varphi)\cos(\theta) \end{pmatrix}$$

Reverse:

$$u, v = \begin{pmatrix} 1 + \text{atan2}(D_x, -D_z) / \pi \\ \text{acos}(D_y) / \pi \end{pmatrix}$$



Skybox

High Dynamic Range

You can find HDR panoramas on Paul Debevec's page:

<http://gl.ict.usc.edu/Data/HighResProbes>

Note:

A HDR skydome can be used as a light source.



Skybox

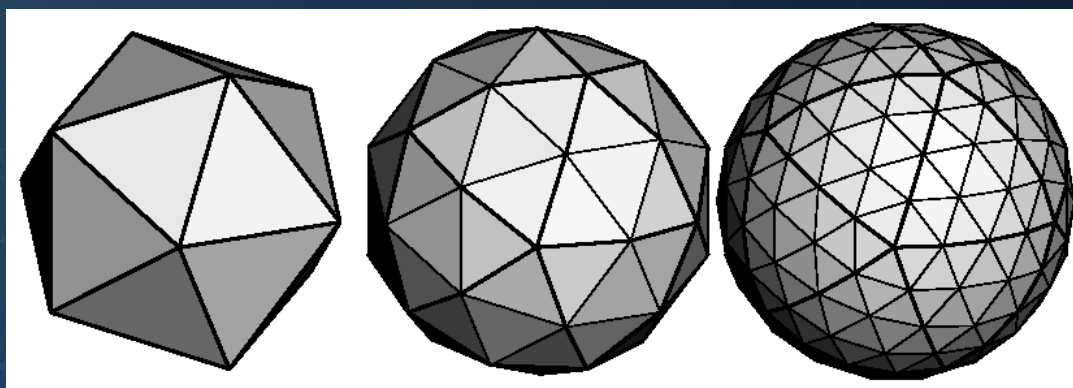
Next Event Estimation for Skydomes

Useful trick:

Use the original skydome only for rays that stumble upon it (implicit light connections).

For next event estimation (*explicit light connections*), use a tessellated (hemi)sphere; assign to each triangle the average skydome color for the directions it covers.

More info on how to do that efficiently: ReSTIR lecture.



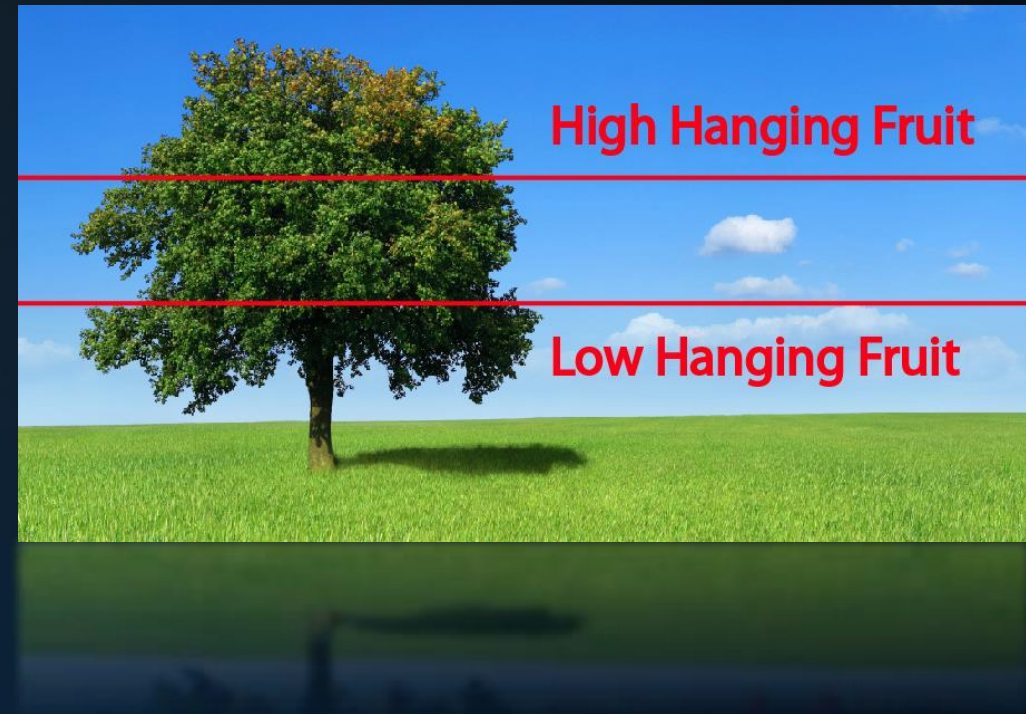
BONUS:

You can now also efficiently importance-sample areas of the skydome.



Today's Agenda:

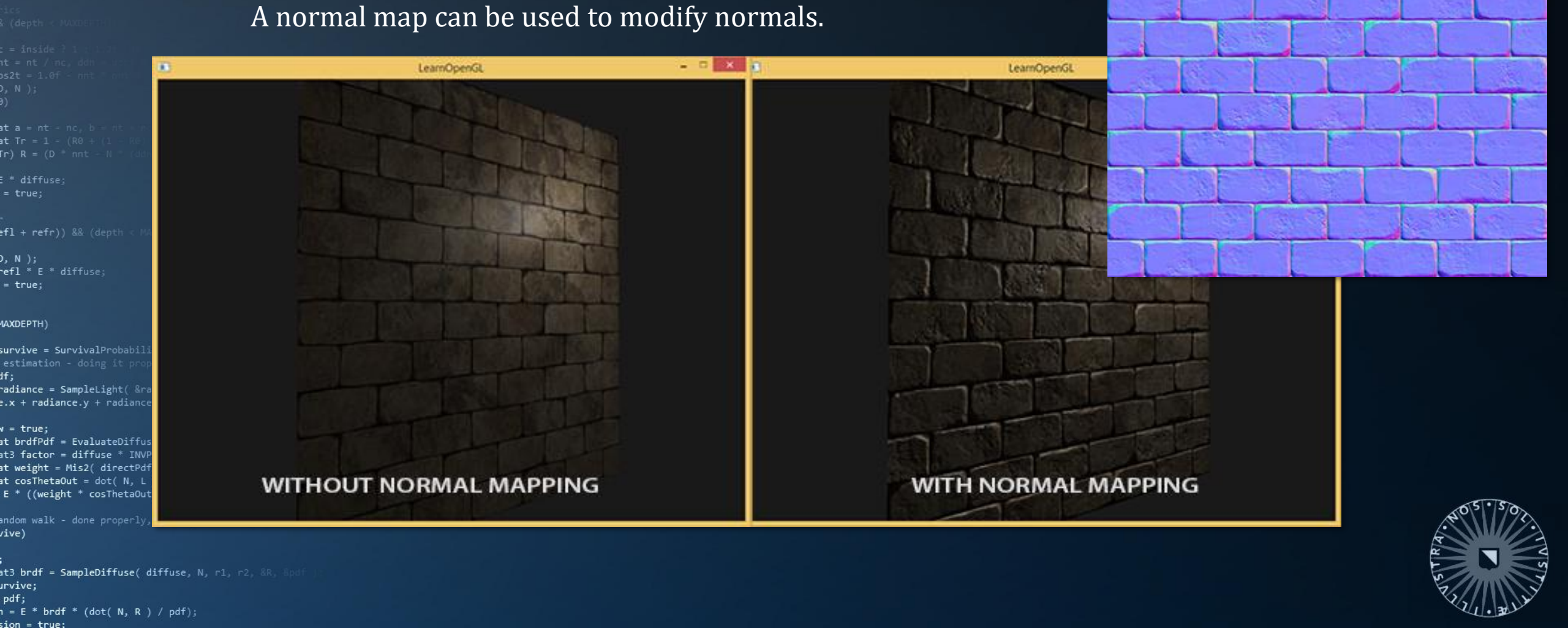
- Gamma Correction
- Depth of Field
- Skybox & IS
- Normal Maps
- Microfacets



Normals

Normal Mapping

A normal map can be used to modify normals.



Normals

Normal Mapping

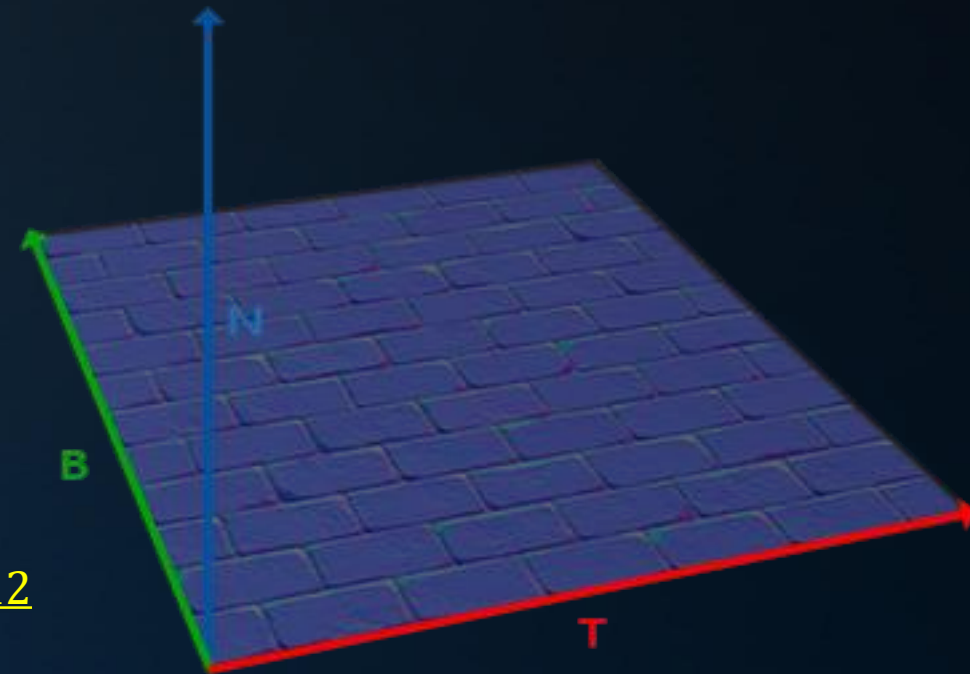
A normal map can be used to modify normals.

This is typically done in tangent space.

Problem: *the orientation of tangent space matters.*

We need to align T and B with the texture, in other words: it needs to be based on the U and V vectors over the surface. This is non-trivial. For a derivation of the calculation of T and B , see:

<https://gamedev.stackexchange.com/questions/68612/how-to-compute-tangent-and-bitangent-vectors>

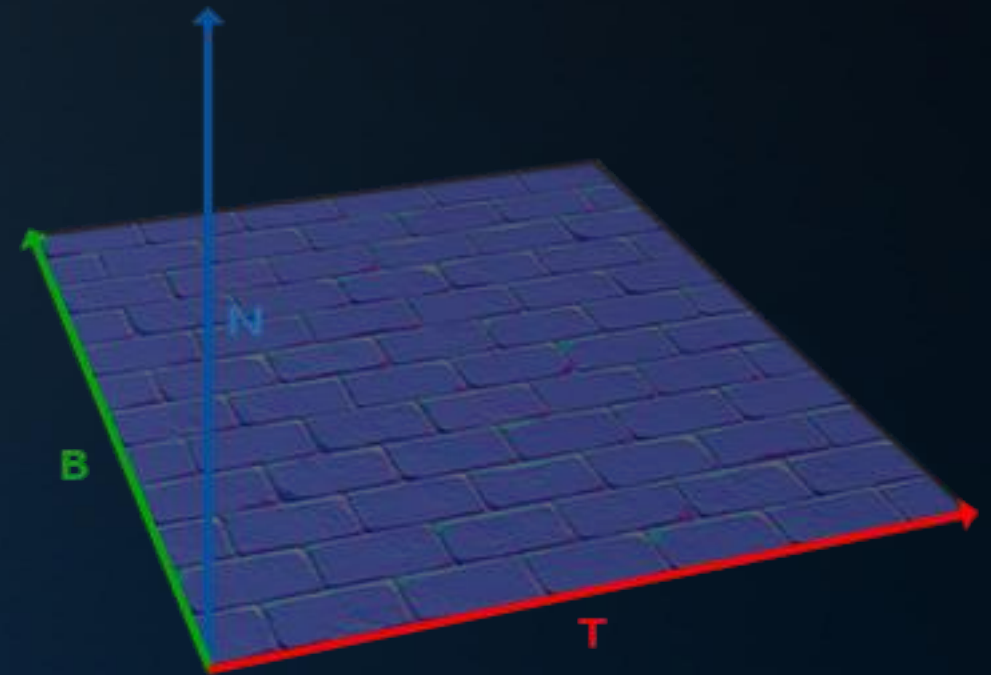


Normals

What if the normal sends you into the surface

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    Tr) R = (D * nnt - N * (ddn * cos2t));
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &lig
    e.x + radiance.y + radiance.z) > 0) && (de
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psu
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf)
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```

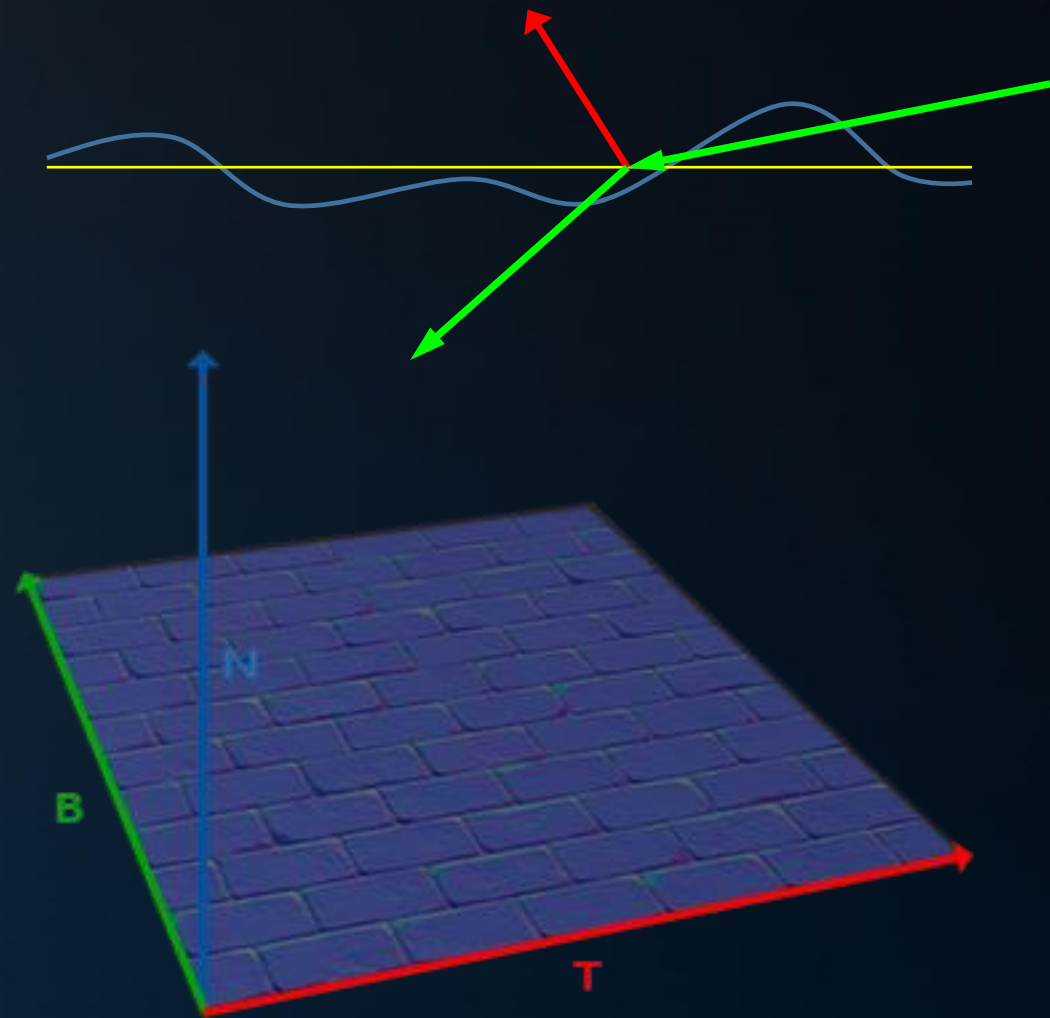


Normals

What if the normal sends you into the surface

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * cos2t);
    Tr) R = (D * nnt - N * (ddn * cos2t));
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lig
    e.x + radiance.y + radiance.z) > 0) && (de
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psu
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf);
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
    
```

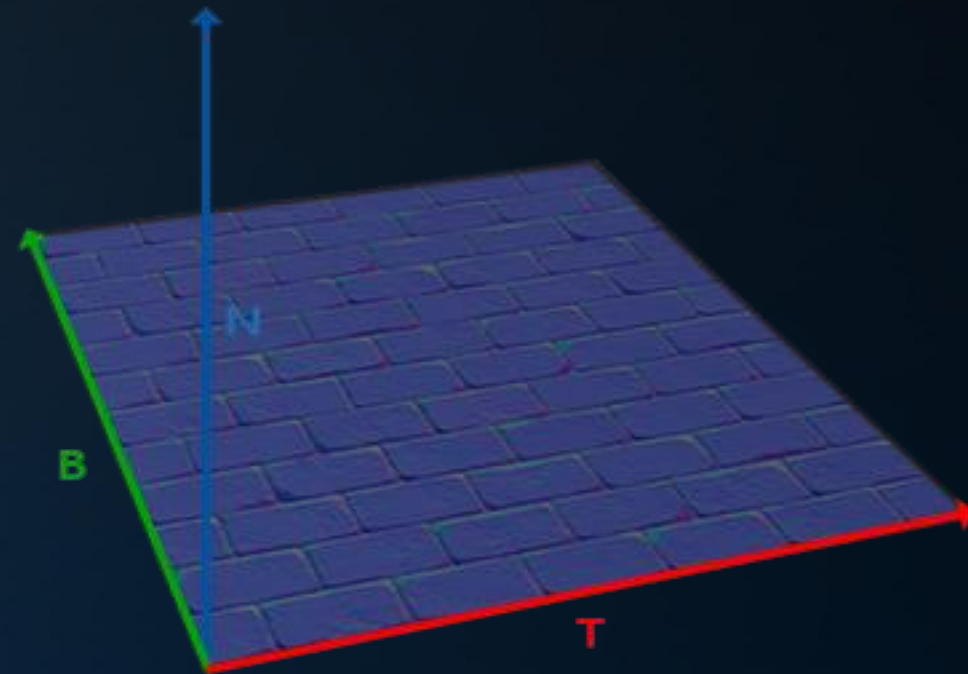
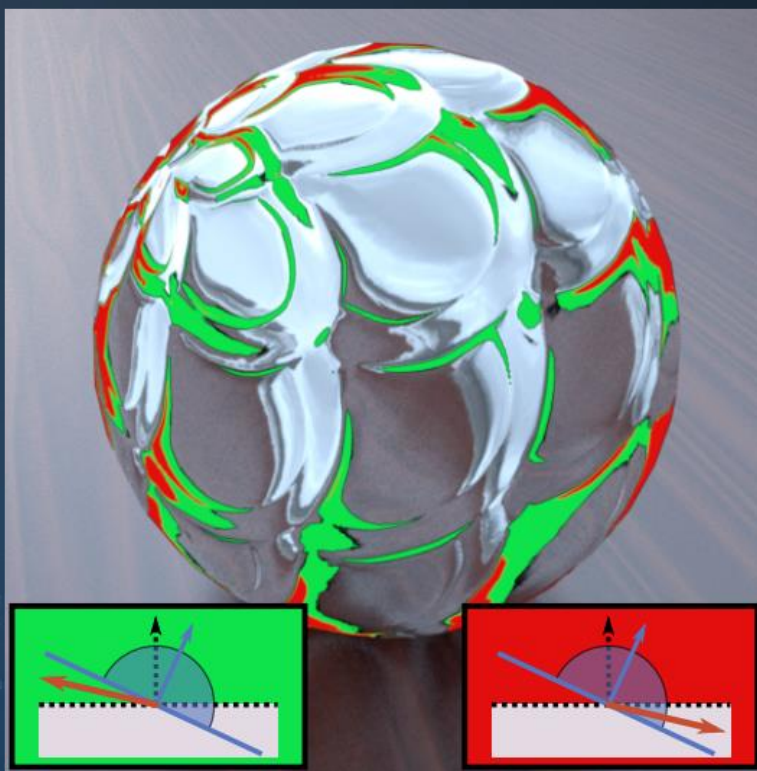


Normals

What if the normal sends you into the surface

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    =
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    df;
    radiance = SampleLight( &rand, I, &L, &lig
    e.x + radiance.y + radiance.z) > 0) && (o
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Pse
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf)
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
  
```



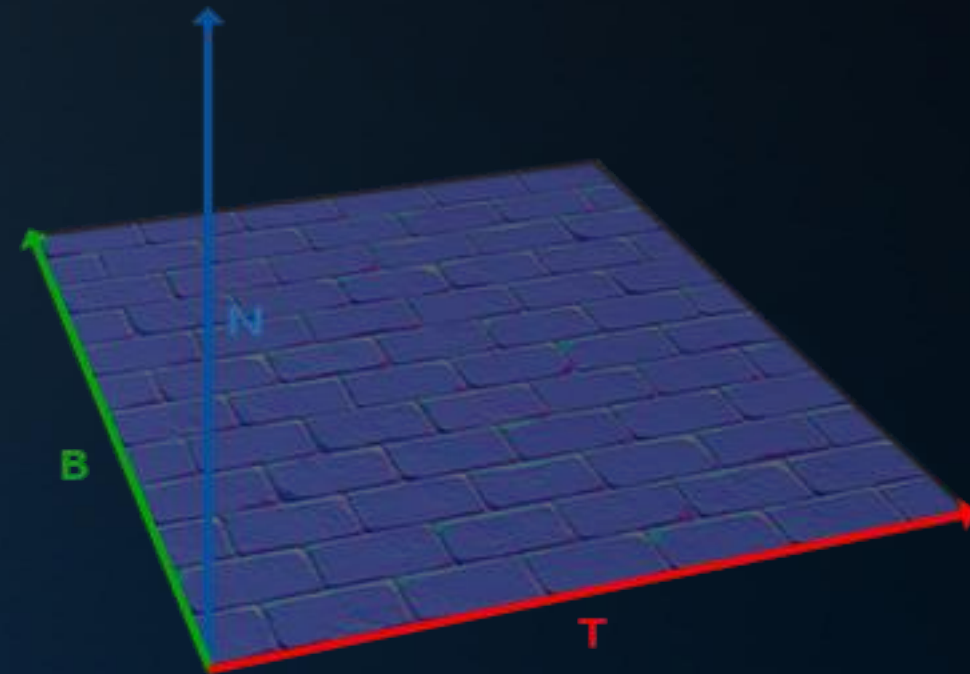
Normals

What if the normal sends you into the surface

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * rand());
        (Tr) R = (D * nnt - N * (ddn * cos2t + 1));
        E * diffuse;
        = true;
    }
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, I,
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lig
    e.x + radiance.y + radiance.z) > 0) && (de
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psu
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf)
    random walk - done properly, closely following
    (survive)
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



Microfacet-based Normal Mapping for Robust Monte Carlo Path Tracing. Schüssler et al., 2017.



Normals

What if the normal sends you into the surface



Microfacet-based Normal Mapping for Robust Monte Carlo Path Tracing. Schüssler et al., 2017.

3.4 Standard Practices for Preventing Artifacts

We compare our model to two techniques that are commonly used in practice to hide the black fringe artifacts of classic normal mapping. Both methods define the BRDF for incident directions below the positive shading hemisphere:

- The *flipping technique* (Figure 4 left) flips the direction of the shading normal. In this way, incident directions always lie in the positive hemisphere of the shading normal and no incident directions are undefined.
- The *switching technique* (Figure 4 right) switches to an alternative, arbitrarily chosen BRDF. We use a diffuse BRDF with albedo $\rho = 0.5$.

To complement the described techniques, we implement a technique suggested by Keller et al. [2017] that mitigates the effect of sampled directions lying below the geometric hemisphere. It works by changing the shading normal such that the reflection vector of the incident direction is always in the positive geometric hemisphere. While this does not prevent invalid directions from being sampled, it ensures that specular reflections do not go below the surface.

All of these techniques modify the BRDF in a way that further amplifies issues with energy conservation and symmetry of classic normal mapping. Further, sampling the adjoints of these techniques is problematic, because the hemisphere (flipping, [Keller et al. 2017]) or the BRDF (switching) may change depending on ω_i . When tracing from the light, we need to sample a ω_i for a given ω_o . Since the hemisphere and BRDF are not fixed before sampling ω_i , choosing a good sampling strategy for ω_i is difficult.

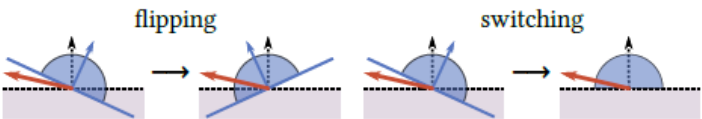


Fig. 4. Standard techniques to prevent undefined directions. The flipping technique (left) changes the orientation of the shading normal if it is backfacing from the incident direction. The switching technique

micro-normal $\omega_t := \omega_p$
Figure 5 shows the results of the V-cavity model for asymmetric cavities.

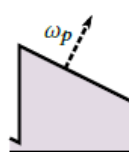


Fig. 5. Microsurface perturbation. The microsurface (shaded) remains the geometric hemisphere.

We have chosen this distribution with minimal area that is similar to the desired normal ω_p has the dominant

- It satisfies the geometric distribution of the microsurface.
- The distribution of the microsurface is such that the final appearance of the microsurface would act as a local specular appearance. The face remains distinct, and frequencies are proportional to the input BRDF.
- This configuration of the desired shading area (in this case) is such that it is proportional to half of the input BRDF, i.e. it does not increase.

4.2 Distribution of Normals

The distribution of normals of the microfacets' is



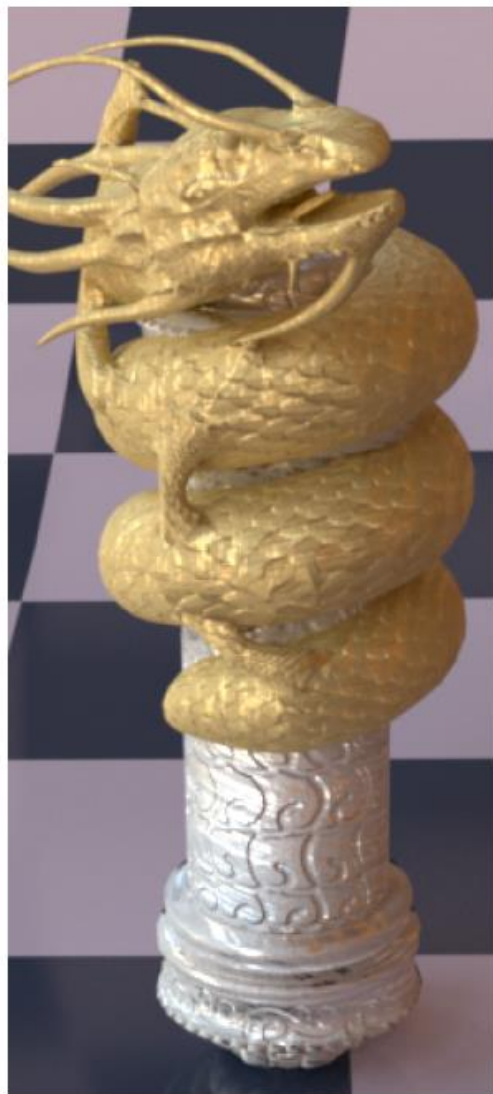
classic
190s

switch (3.4)
194s

flip (3.4)
192s

2nd-order scattering
203s using Algo. 2
202s using Eq. (23)

∞ th-order scattering
211s

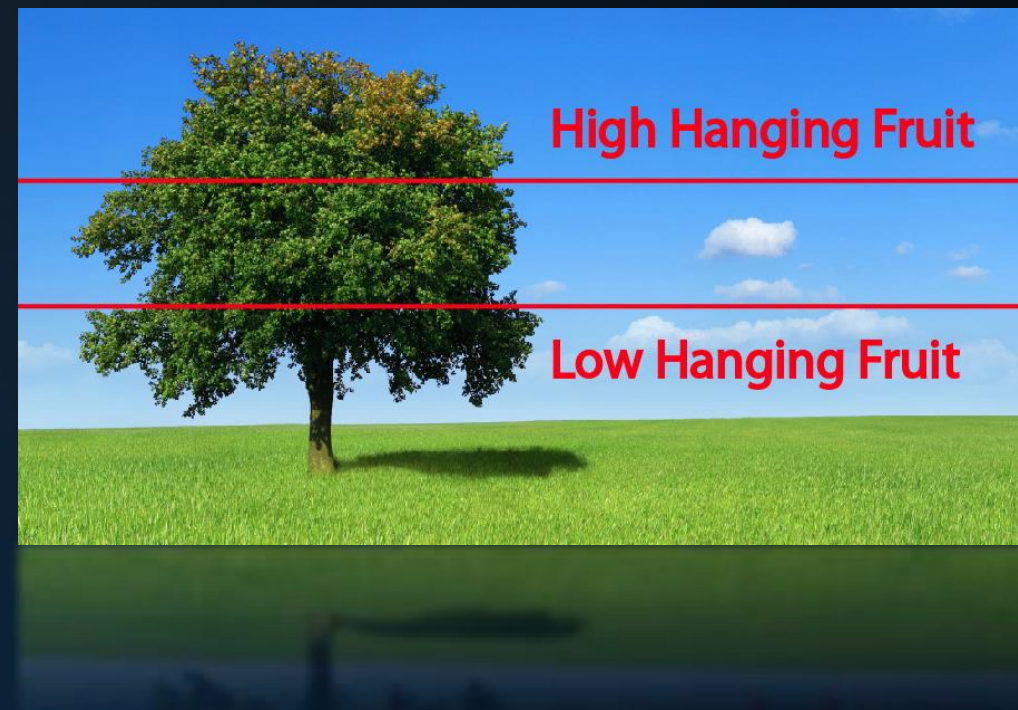


```
res = brdf * sampleRuse( distRuse, N, R );  
survive;  
pdf;  
n = E * brdf * (dot( N, R ) / pdf);  
sion = true;
```



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox & IS
- Normal Maps
- Microfacets



Microfacet

BRDFs Without Issues

We have two BRDFs without problems:

1. The Lambertian BRDF
2. The pure specular BRDF

These are physically plausible and can be sampled. The PDF is also clear.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, N);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightDir,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small's
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```



Microfacet

Microfacet BRDFs*

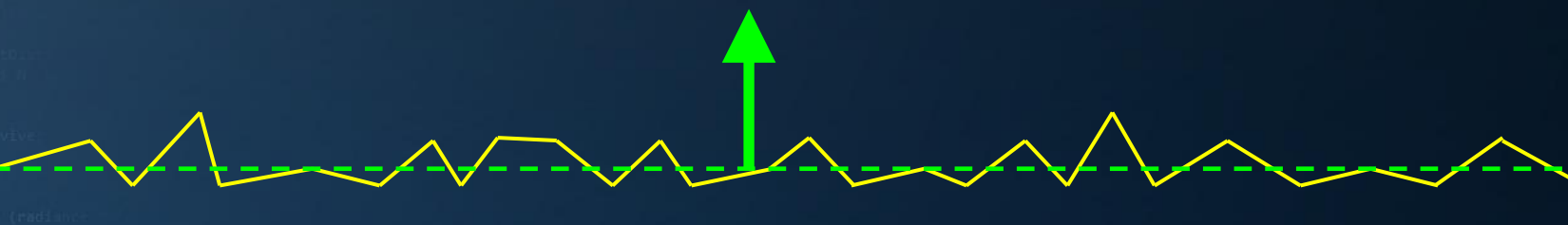
We can simulate a broad range of materials if we assume:
at a microscopic level, the material consists of tiny specular fragments.

- If the fragment orientations are chaotic, the material appears diffuse.
- If the fragment orientations are all the same, the material appears specular.
- Different but similar orientations yield glossy materials.



```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, N);
        cos2t = 1.0f - nnt * ddn;
        D, N );
    }
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse,
    estimation - doing it properly, closely
    if;
    radiance = SampleLight( &rand, I, &L, &light;
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following SampleSurvive)
    survive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2);
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;
  
```



*: Torrance & Sparrow, Theory for Off-Specular Reflection from Roughened Surfaces. 1967.



Microfacet BRDFs*

$$f_r(\vec{L}, \vec{V}) = \frac{F(\vec{L}, \vec{V})G(\vec{L}, \vec{V}, \vec{H})D(\vec{H})}{4(\vec{N} \cdot \vec{L})(\vec{N} \cdot \vec{V})}$$

1. Normal distribution D
2. Geometry term G
3. Fresnel term F
4. Normalization



Microfacet

Normal Distribution

$$f_r(x, \theta_i, \theta_o) = \frac{L_o(x, \theta_o)}{L_i(x, \theta_i) \cos \theta_i}$$

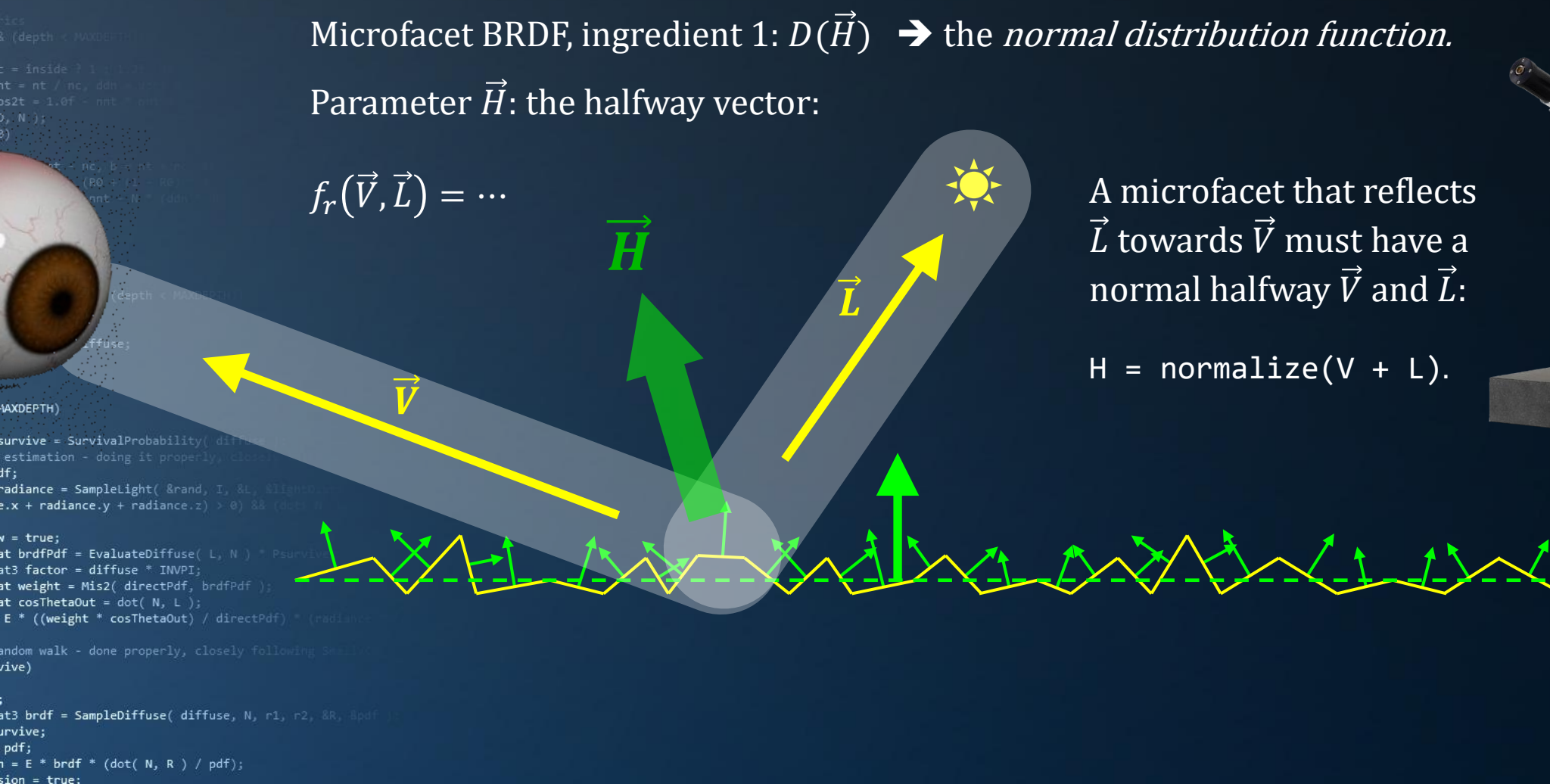
Microfacet BRDF, ingredient 1: $D(\vec{H}) \rightarrow$ the *normal distribution function*.

Parameter $\vec{H}$: the halfway vector:

$$f_r(\vec{V}, \vec{L}) = \dots$$

A microfacet that reflects $\vec{L}$ towards $\vec{V}$ must have a normal halfway $\vec{V}$ and $\vec{L}$:

$$\vec{H} = \text{normalize}(\vec{V} + \vec{L}).$$



Microfacet

```

ics
& (depth < MAXDEPTH)
{
    // Inside?
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }

    // ...
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * ddn);
    (Tr) R = (D * nnt + N * (ddn > 0 ? 1 : -1));

    // ...
    E * diffuse;
    = true;

    // ...
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

        // ...
    }
}

MAXDEPTH)
{
    survive = SurvivalProbability( diffuse );
    // estimation - doing it properly, closely following
    if
    {
        radiance = SampleLight( &rand, I, &L, &align;
        e.x + radiance.y + radiance.z) > 0) && (depth <
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }

    // random walk - done properly, closely following Small's
    (survive)
    {
        // ...
        at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
        survive;
        pdf;
        n = E * brdf * (dot( N, R ) / pdf);
        // ...
    }
}

```

Normal Distribution

Intuitive choices for D:

$D(\vec{H}) = C$: microfacet normals are equally distributed → diffuse material.

$D(\vec{H}) = \begin{cases} \infty, & \text{for } \vec{H} = (0,0,1) \\ 0, & \text{otherwise} \end{cases}$: all microfacet normals are (0,0,1) → pure specular.

Good practical choice for D: the Blinn-Phong distribution;

$$D(\vec{H}) = \frac{\alpha + 2}{2\pi} \underline{(\vec{N} \cdot \vec{H})}^{\alpha}$$



Microfacet

Geometry Term

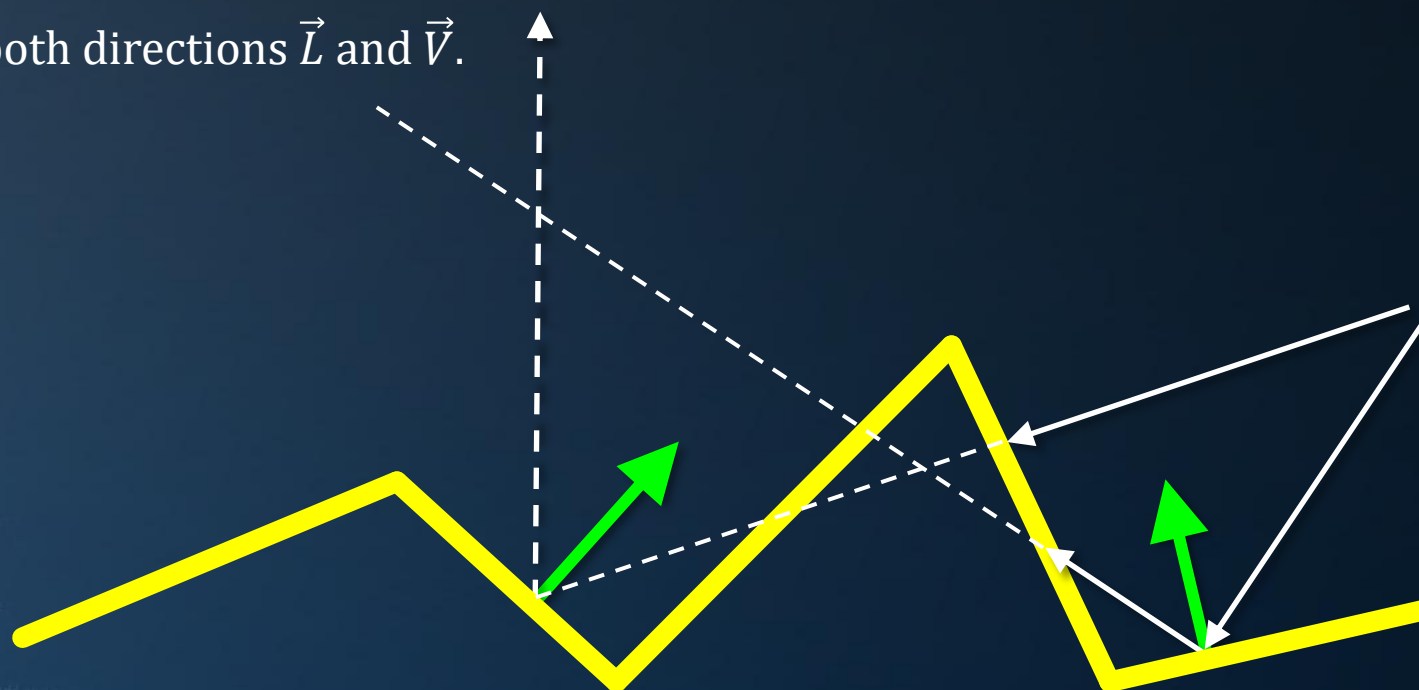
Microfacet BRDF, ingredient 2: $G(\vec{V}, \vec{L}, \vec{H}) \rightarrow$ the *geometry term*.

It describes what fraction of a microsurface with normal $\vec{H}$ is visible in both directions $\vec{L}$ and $\vec{V}$.

Geometry Term

Microfacet BRDF, ingredient 2: $G(\vec{V}, \vec{L}, \vec{H}) \rightarrow$ the *geometry term*.

It describes what fraction of a microsurface with normal $\vec{H}$ is visible in both directions $\vec{L}$ and $\vec{V}$.



Microfacet

Geometry Term

Intuitive choice for G:

$G(\vec{V}, \vec{L}, \vec{H}) = 1$: no occlusion.

Good practical choice for G*:

$$G(\vec{V}, \vec{L}, \vec{H}) = \min(1, \min\left(\frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{V})}{\vec{V} \cdot \vec{H}}, \frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{L})}{\vec{V} \cdot \vec{H}}\right))$$

*: Physically Based Rendering, page 455



Microfacet

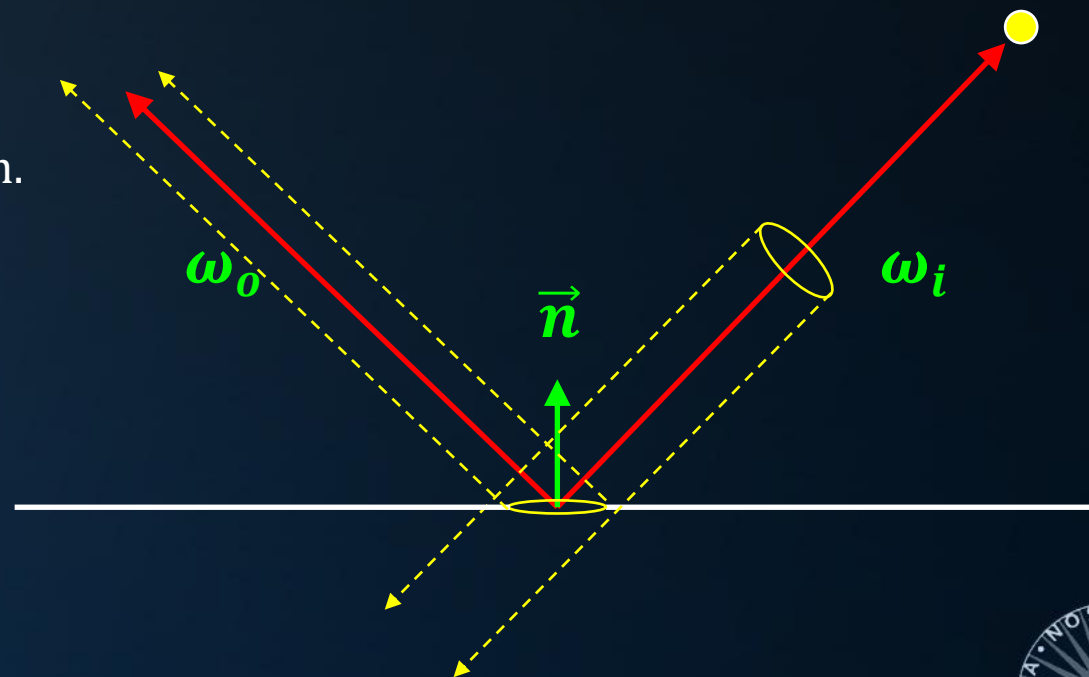
Fresnel Term

Microfacet BRDF, ingredient 3: $F(\vec{L}, \vec{H}) \rightarrow$ the *Fresnel term*.

So far, we assumed that the light reflected by a specular surface is only modulated by the material color.

This is not true for dielectrics: here we use the Fresnel equations to determine reflection.

In nature, Fresnel does not just apply to dielectrics.



Microfacet

Fresnel Term

Iron is specular, but reflectivity differs depending on incident angle.

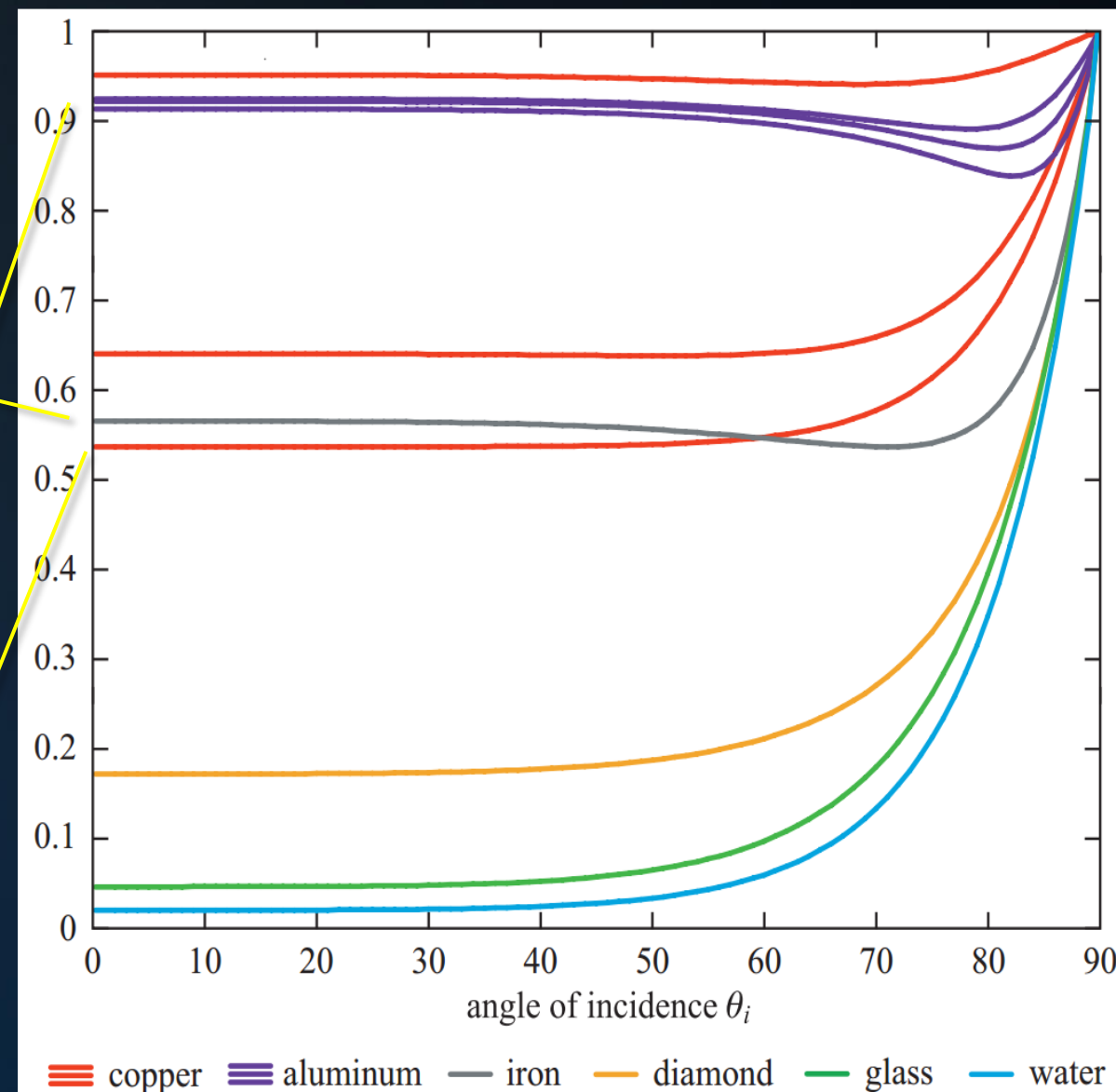
Aluminum is even more interesting: reflectivity depends on wavelength. The three lines in the graph:

Top: blue, middle: green, bottom: red.

Copper takes this to extremes: at grazing angles, it appears white. The lines in the graph:

Top: red, middle: green, bottom: blue.

(hence its reddish appearance)



From "Real-time Rendering, 3rd edition, A. K. Peters.

Microfacet

Fresnel Term

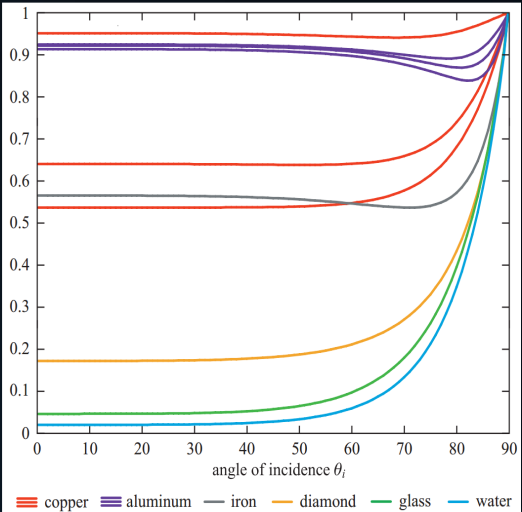
For Fresnel, we use Schlick’s approximation:

$$F_r = k_{specular} + (1 - k_{specular})(1 - (\vec{L} \cdot \vec{H}))^5$$

Note that this is calculated per color channel ($k_{specular}$ is an rgb triplet).

Values for $k_{specular}$ for various materials:

Iron	0.56, 0.57, 0.58
Copper	0.95, 0.64, 0.54
Gold	1.00, 0.71, 0.29
Aluminum	0.91, 0.92, 0.92
Silver	0.95, 0.93, 0.88



Microfacet

Bringing it All Together

The Microfacet BRDF:

$$f_r(\vec{L}, \vec{V}) = \frac{F(\vec{L}, \vec{V})G(\vec{L}, \vec{V}, \vec{H})D(\vec{H})}{4(\vec{N} \cdot \vec{L})(\vec{N} \cdot \vec{V})}$$

$$D(\vec{H}) = \frac{\alpha + 2}{2\pi} \frac{(\vec{N} \cdot \vec{H})^\alpha}{}$$

$$G(\vec{V}, \vec{L}, \vec{H}) = \min(1, \min\left(\frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{V})}{\vec{V} \cdot \vec{H}}, \frac{2(\vec{N} \cdot \vec{H})(\vec{N} \cdot \vec{L})}{\vec{V} \cdot \vec{H}}\right))$$

For a full derivation of the denominator of the BRDF, see Physically Based Rendering, section 8.4.2.

$$F_r = k_{specular} + (1 - k_{specular})(1 - (\vec{L} \cdot \vec{H}))^5$$

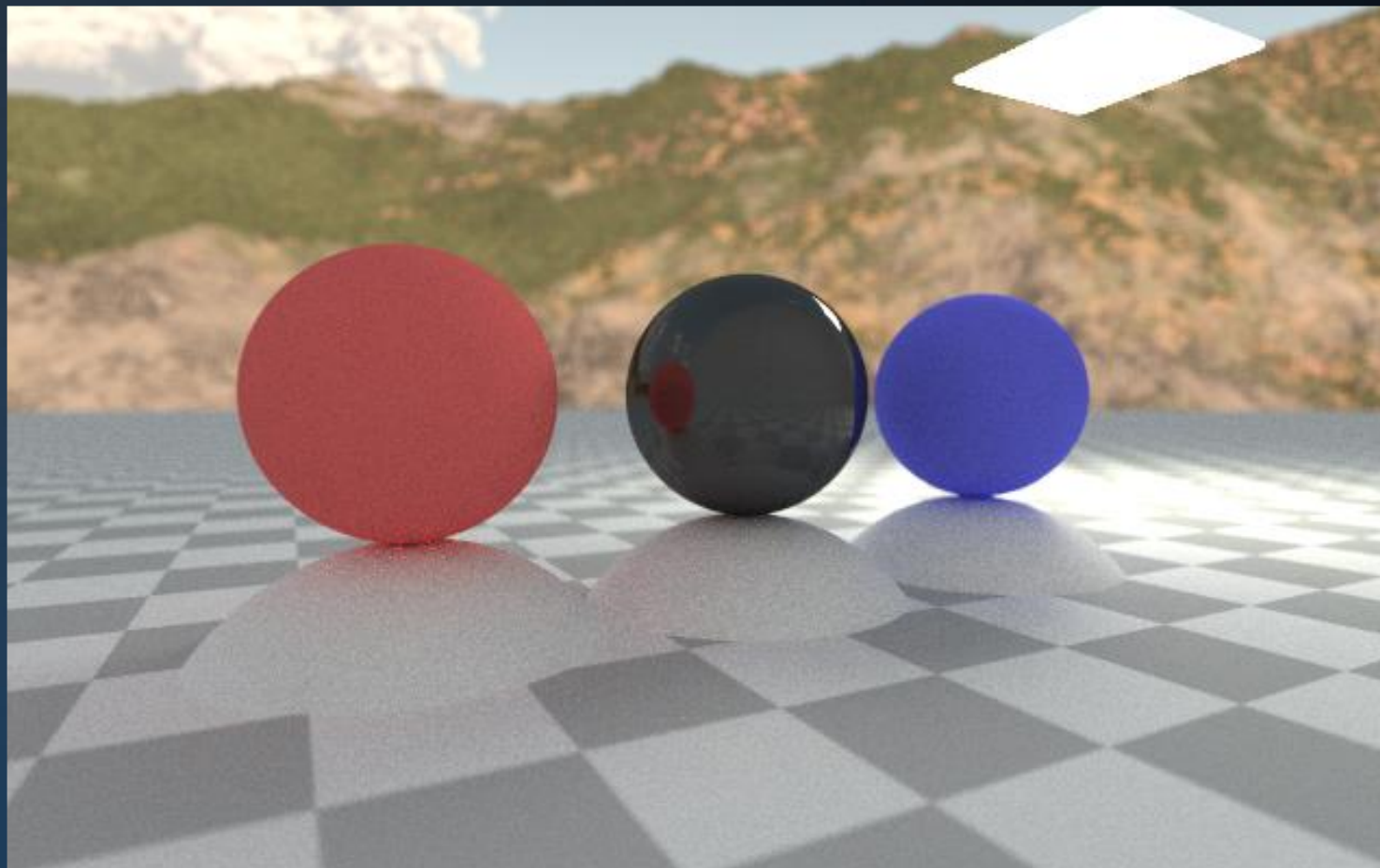


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0.5)
    {
        nt = nt / nc, ddn = ddn / nc;
        r = 1.0f - nnt * ddn;
        r = (D, N);
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * r);
        Tr = (D * nnt - N * (ddn * r));
    }
    E * diffuse;
    = true;
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N);
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z) > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    (survive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;

```



Lambertian BRDF

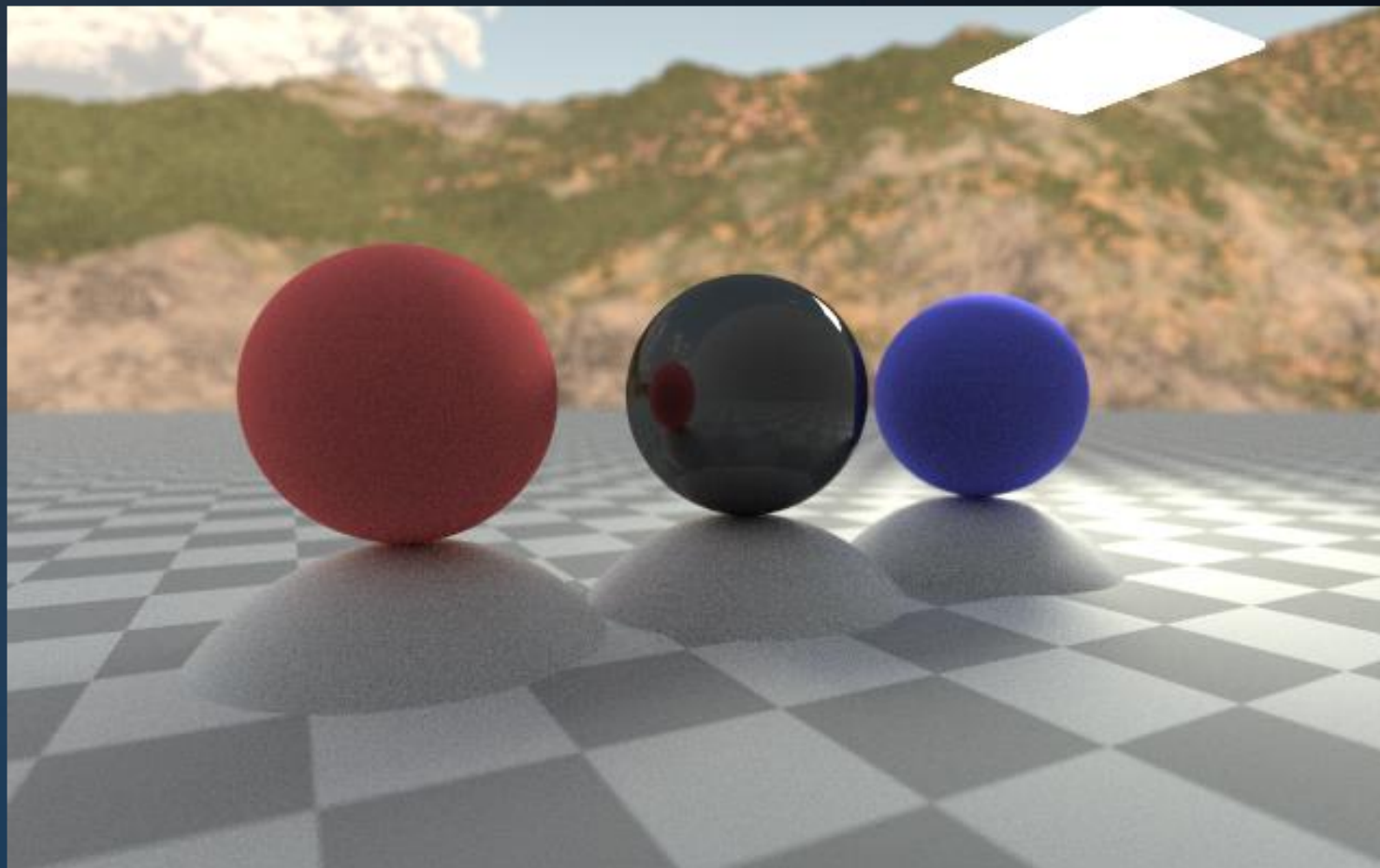


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = dot(N, D);
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    else
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        (Tr) R = (D * nnt - N * (ddn < 0 ? 1 : -1));
        E * diffuse;
        = true;
    }
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    if;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Small
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    ion = true;

```



Blinn-Phong Microfacet BRDF, $\alpha=1$



```

115
k (depth < MAXDEPTH)
{
    if (nt < inside) { 1; nnt = nnt * nc;
    nt = nt / nc; ddn = ddn * nc;
    nnt = nnt * nc; ddn = ddn * nc;
    ps2t = 1.0f - nnt * ddn;
    D, N );
    0);
    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * a);
    Fr) R = (D * nnt - N * (ddn *
    E * diffuse;
    = true;
    -
    efl + refr)) && (depth < MAXDEPTH)
    D, N );
    refl * E * diffuse;
    = true;
    MAXDEPTH)
    survive = SurvivalProbability( diffuse, N,
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &lightD,
    e.x + radiance.y + radiance.z) > 0) && (out.N
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following Seelye
    vive)
    ;
    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

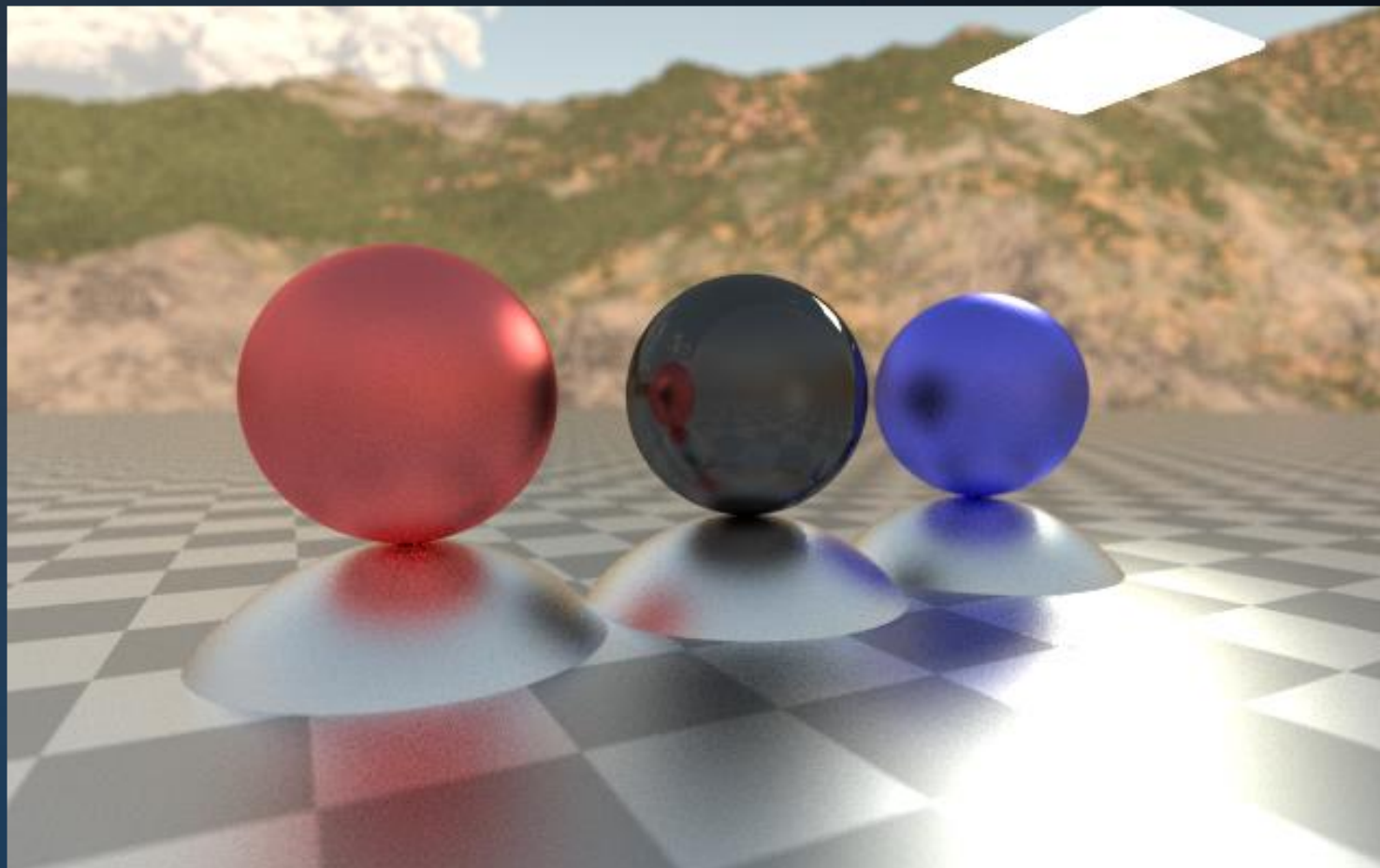


Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc, ddn = ddn * nc;
        cos2t = 1.0f - nnt * nnt;
        D, N );
    }
    {
        at a = nt - nc, b = nt + nc;
        at Tr = 1 - (R0 + (1 - R0) * ddn);
        (Tr) R = (D * nnt - N * (ddn > 0 ? 1 : -1));
    }
    E * diffuse;
    = true;
    {
        refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;
    }
    MAXDEPTH)
    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &align, &pdf );
    e.x + radiance.y + radiance.z > 0) && (depth < MAXDEPTH)
    {
        w = true;
        at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
        at3 factor = diffuse * INVPI;
        at weight = Mis2( directPdf, brdfPdf );
        at cosThetaOut = dot( N, L );
        E * ((weight * cosThetaOut) / directPdf) * (radiance
    }
    random walk - done properly, closely following Small's
    (survive)
    {
        at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
        survive;
        pdf;
        n = E * brdf * (dot( N, R ) / pdf);
        sion = true;
    }
}

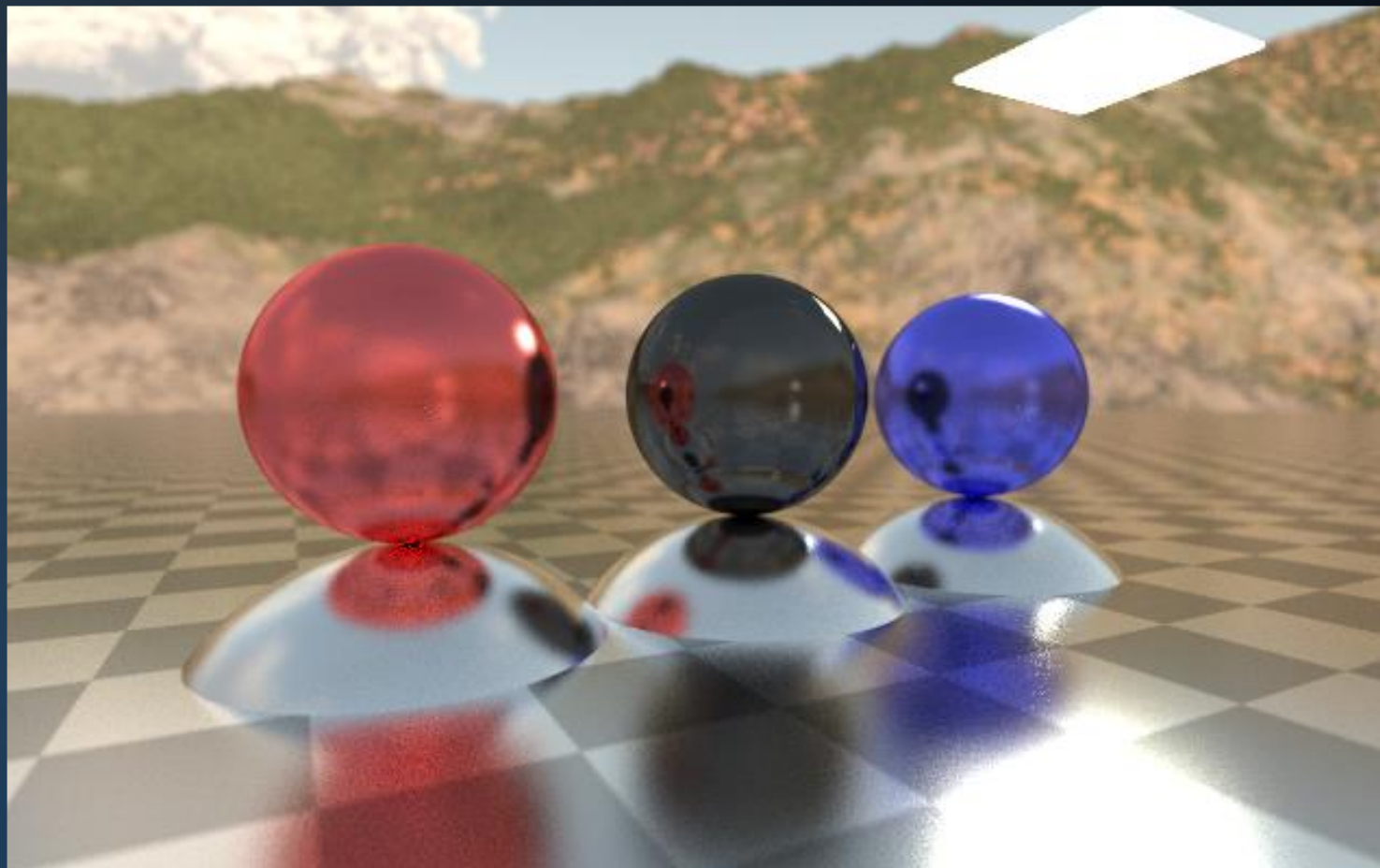
```



Blinn-Phong Microfacet BRDF, $\alpha=50$



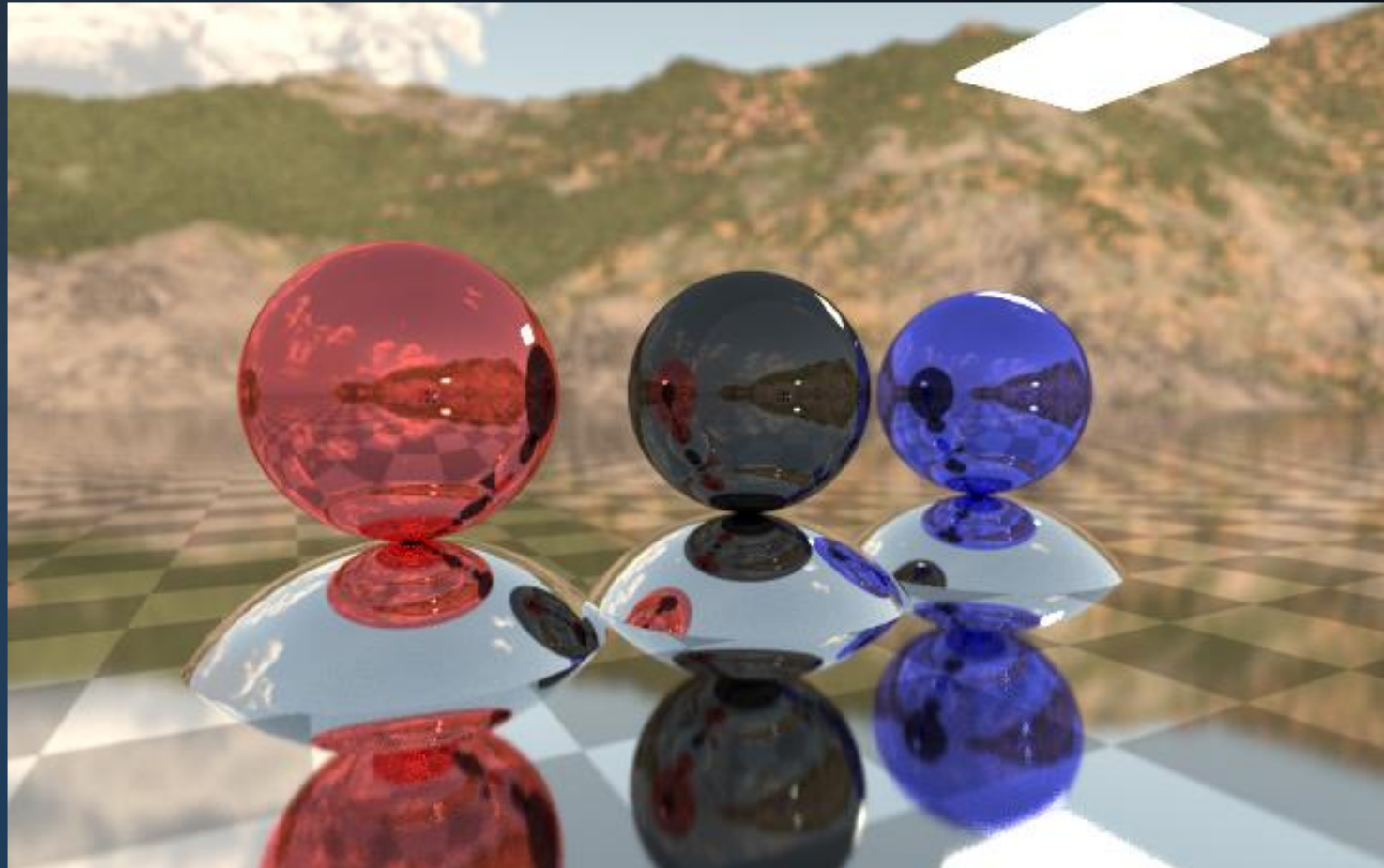
Microfacet



Blinn-Phong Microfacet BRDF, $\alpha=500$



Microfacet



Blinn-Phong Microfacet BRDF, $\alpha=50000$



Microfacet

```

ics
& (depth < MAXDEPTH)
{
    if (inside ? 1 : 0)
    {
        nt = nt / nc; ddn = ddn * nt;
        r = 1.0f - nnt * nnt;
        D, N );
    }

    at a = nt - nc, b = nt + nc;
    at Tr = 1 - (R0 + (1 - R0) * r);
    Tr) R = (D * nnt - N * (ddn * r));

    E * diffuse;
    = true;

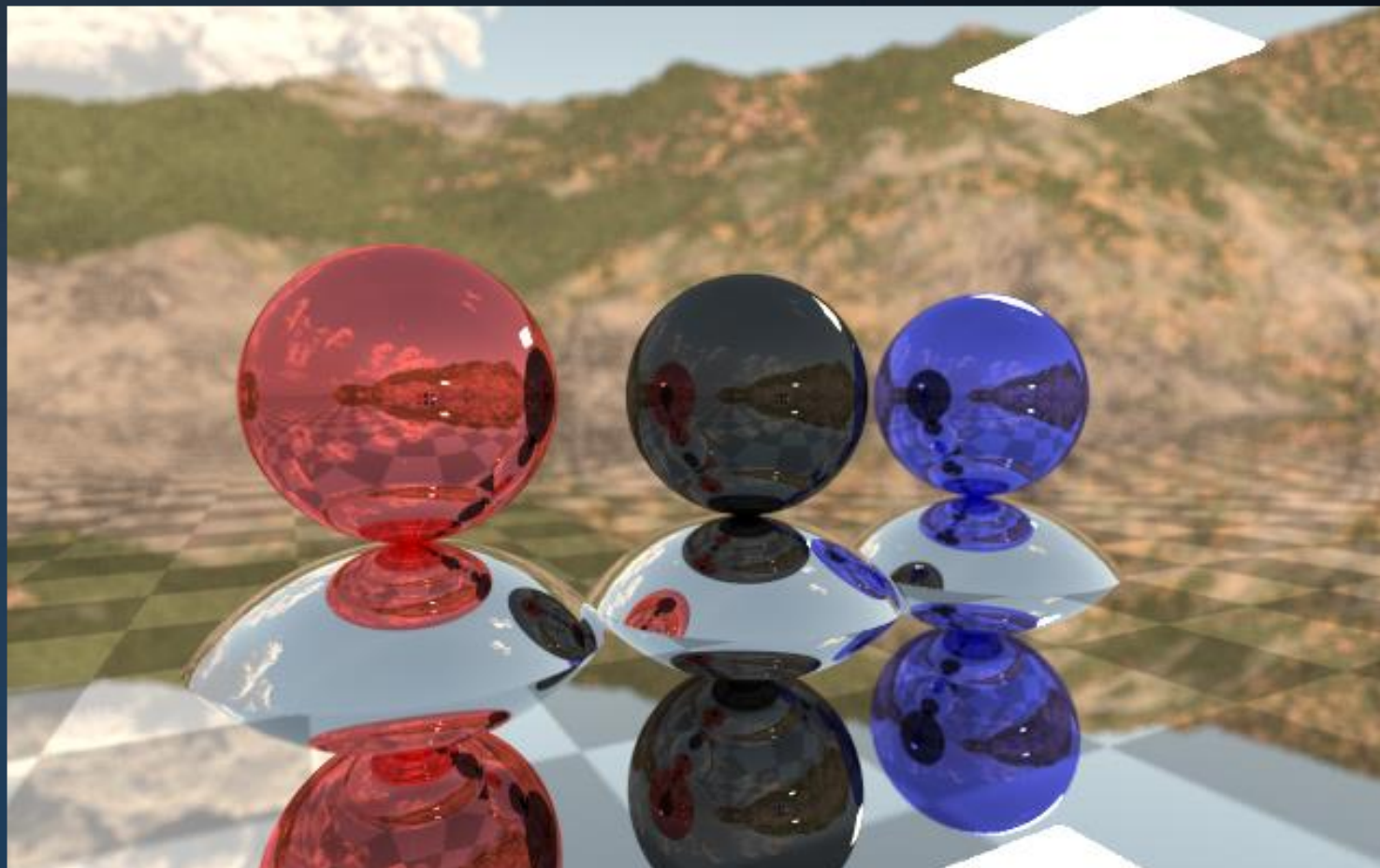
    refl + refr)) && (depth < MAXDEPTH)
    {
        D, N );
        refl * E * diffuse;
        = true;

    MAXDEPTH)

    survive = SurvivalProbability( diffuse );
    estimation - doing it properly, closely following
    df;
    radiance = SampleLight( &rand, I, &L, &light,
    e.x + radiance.y + radiance.z) > 0) && (depth <
    w = true;
    at brdfPdf = EvaluateDiffuse( L, N ) * Psurvive;
    at3 factor = diffuse * INVPI;
    at weight = Mis2( directPdf, brdfPdf );
    at cosThetaOut = dot( N, L );
    E * ((weight * cosThetaOut) / directPdf) * (radiance
    random walk - done properly, closely following
    survive)

    at3 brdf = SampleDiffuse( diffuse, N, r1, r2, &R, &pdf );
    survive;
    pdf;
    n = E * brdf * (dot( N, R ) / pdf);
    sion = true;

```

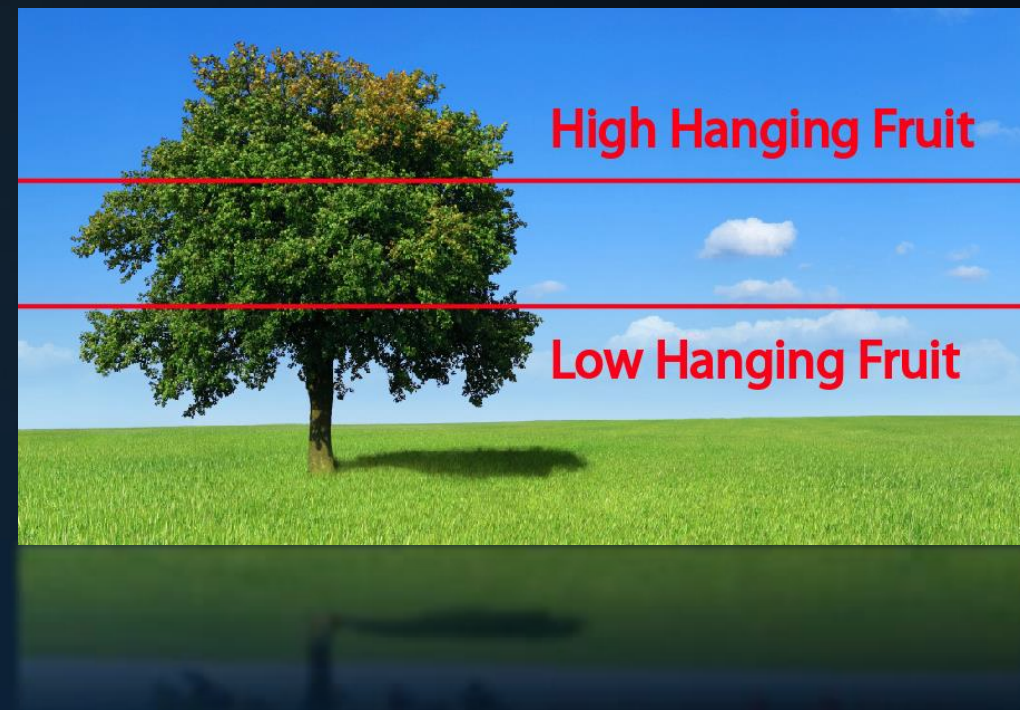


Specular BRDF



Today's Agenda:

- Gamma Correction
- Depth of Field
- Skybox & IS
- Normal Maps
- Microfacets



INFOMAGR – Advanced Graphics

Jacco Bikker - November 2022 - February 2023

END of “Various”

next: Assignment 2 deadline, then: Christmas Break

